



EDMI Microsystems and Microelectronics

MICRO-614: Electrochemical Nano-Bio-Sensing
and Bio/CMOS interfaces

Lecture #4

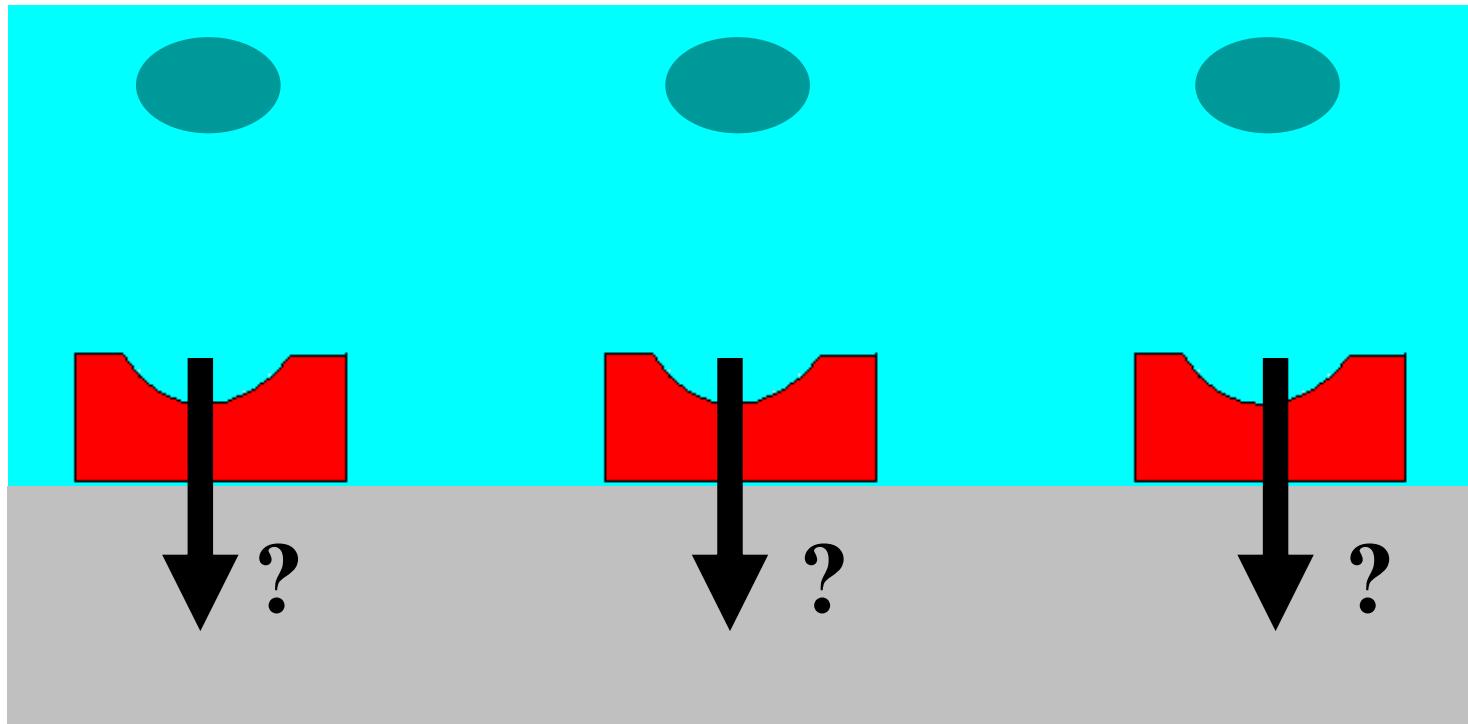
Probe Detection Principles (DNA, Antibodies & Oxidases)

Lecture Outline

(Book Bio/CMOS: Chapter 5)

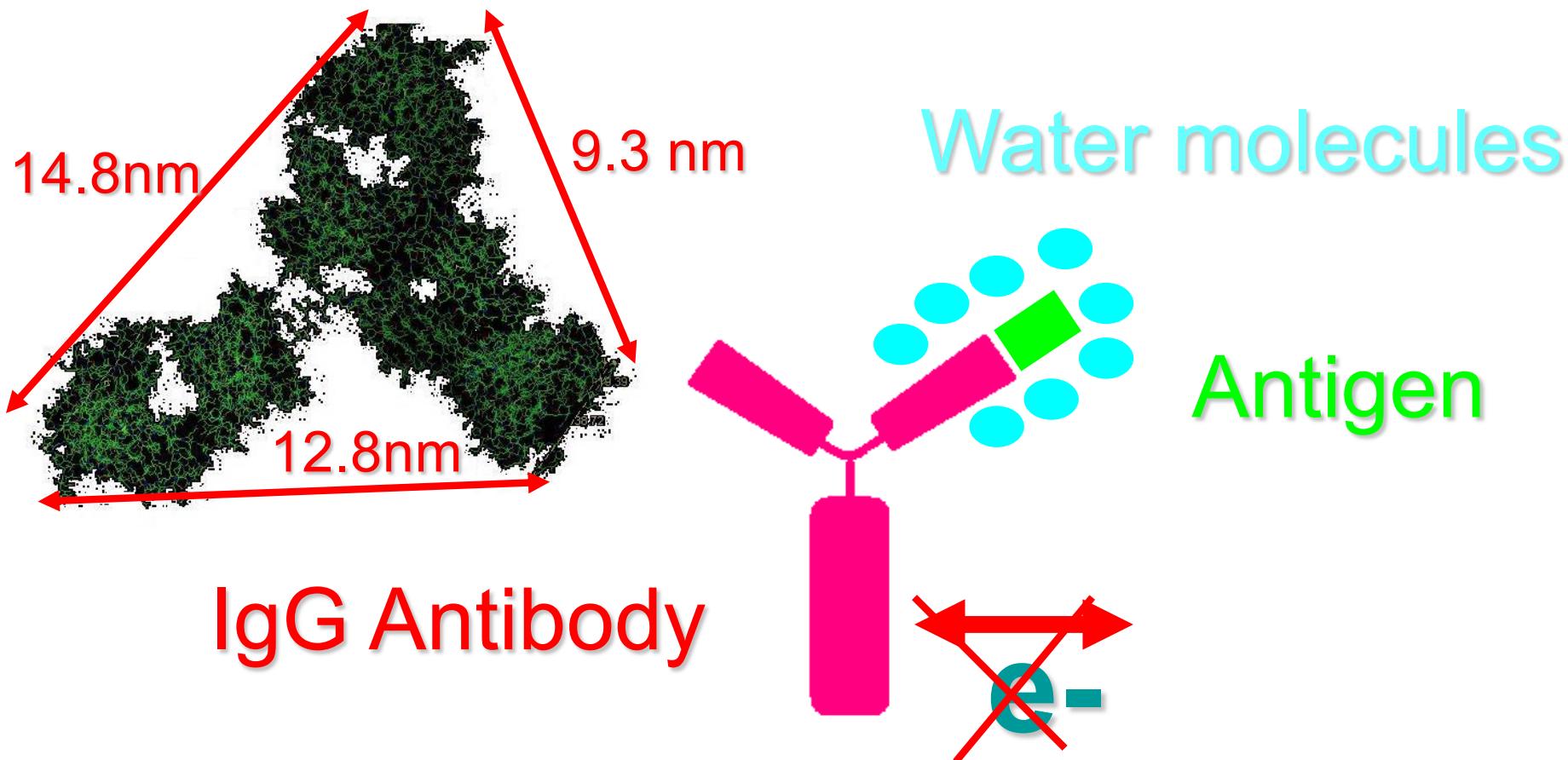
- DNA hybridization at Bio/CMOS interface
- Impedimetric Detection
- Capacitive Detection
- Layering effects
- Helmholtz Planes & Debye Length
- Amperometric Detection

CMOS/Sample interface



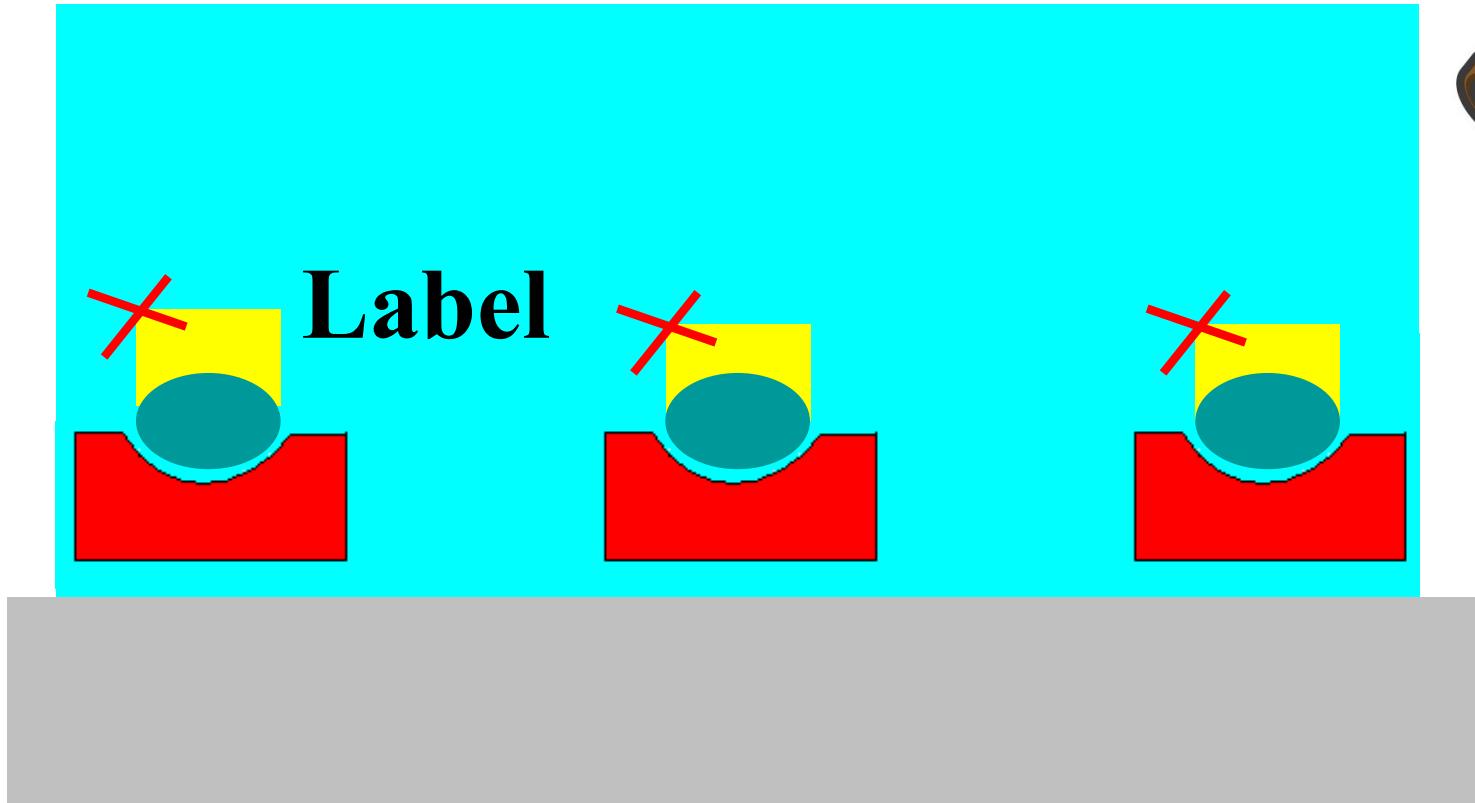
The interface between the CMOS circuit and the bio-sample needs to be deeply investigated and organized

The interaction IgG-Ag



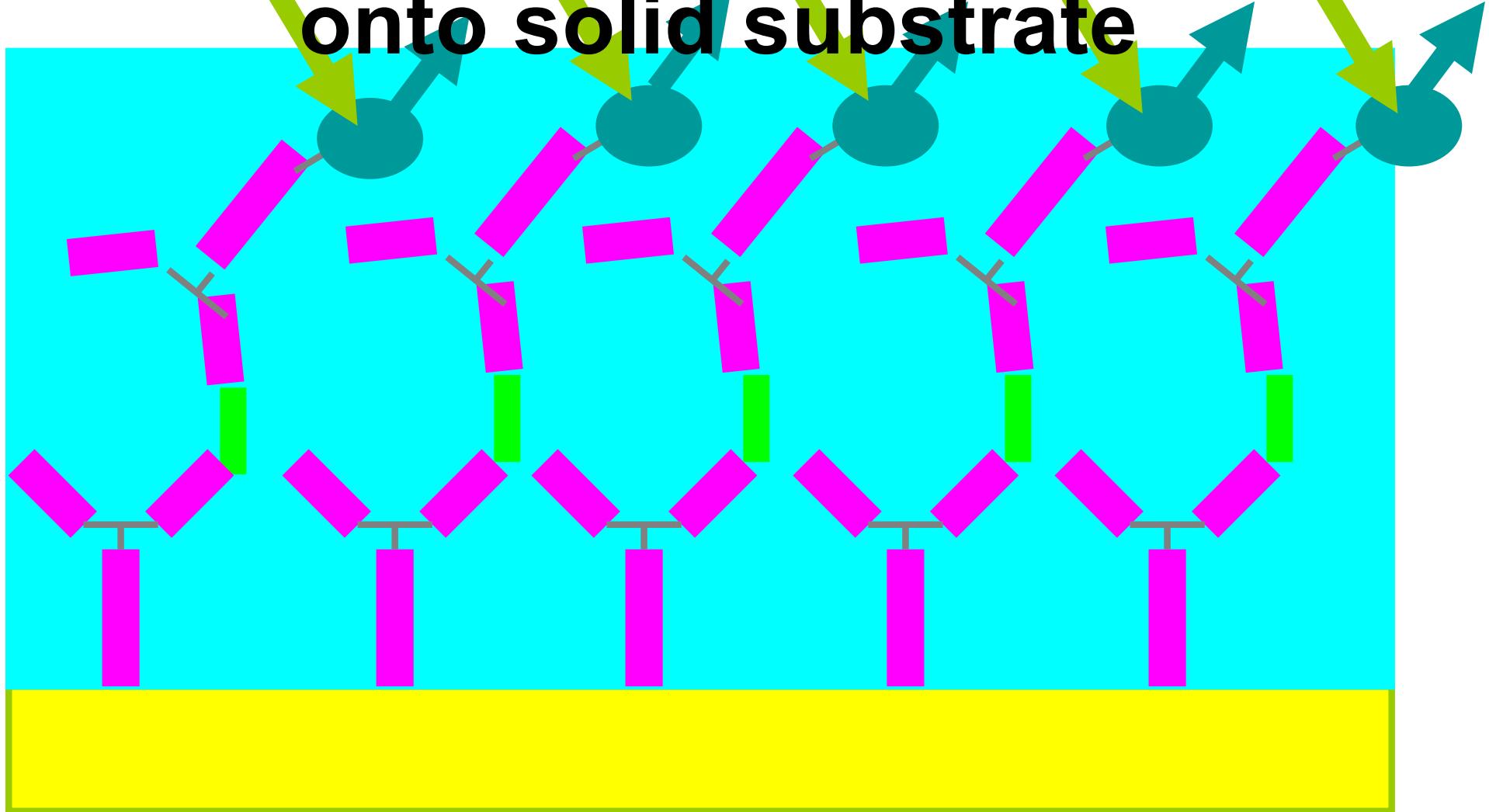
The antigen rests in a very tight binding pocket which is exactly the right size and shape to receive it. Other important factors include enthalpic contributions from van der Waals interactions and hydrogen bonds, and entropic contributions from the release of bound water upon antigen binding

Measuring Bio-Markers



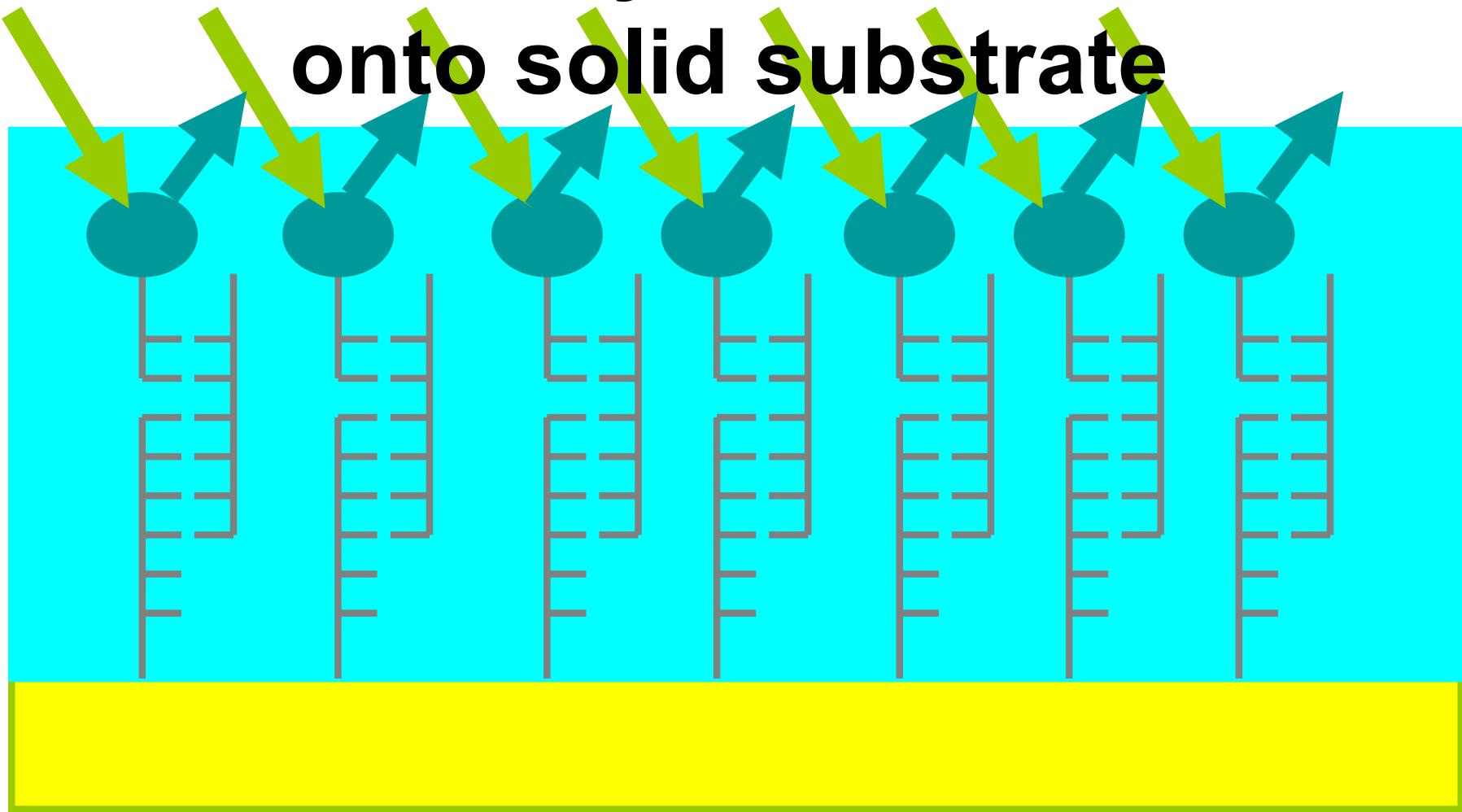
The Measure of Bio-markers may be performed in a labeled manner or in label-free mode

Antibody-Antigen up-take onto solid substrate



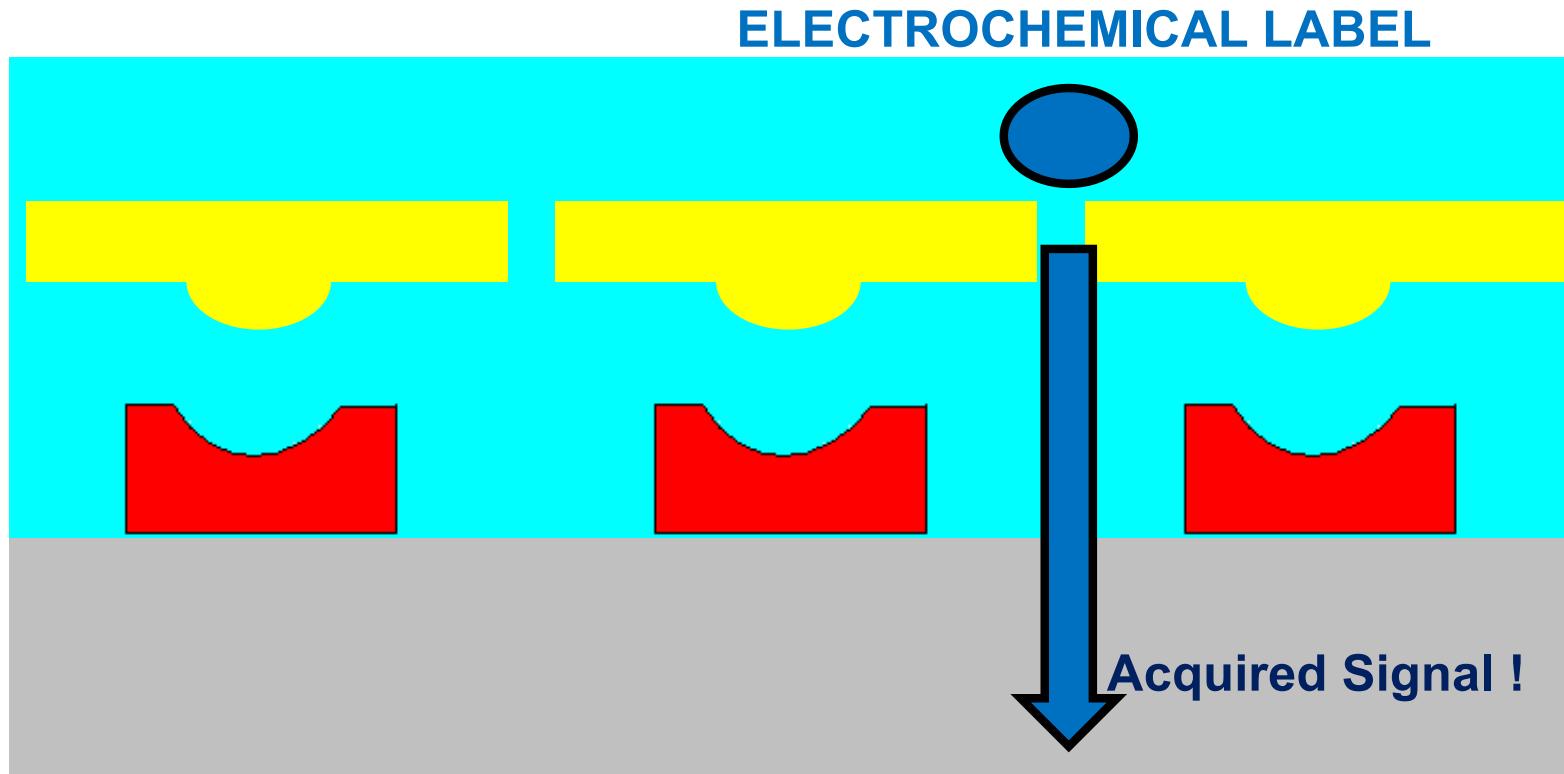
Antigens are specific detected by
immobilizing the right antibodies

DNA hybridization onto solid substrate



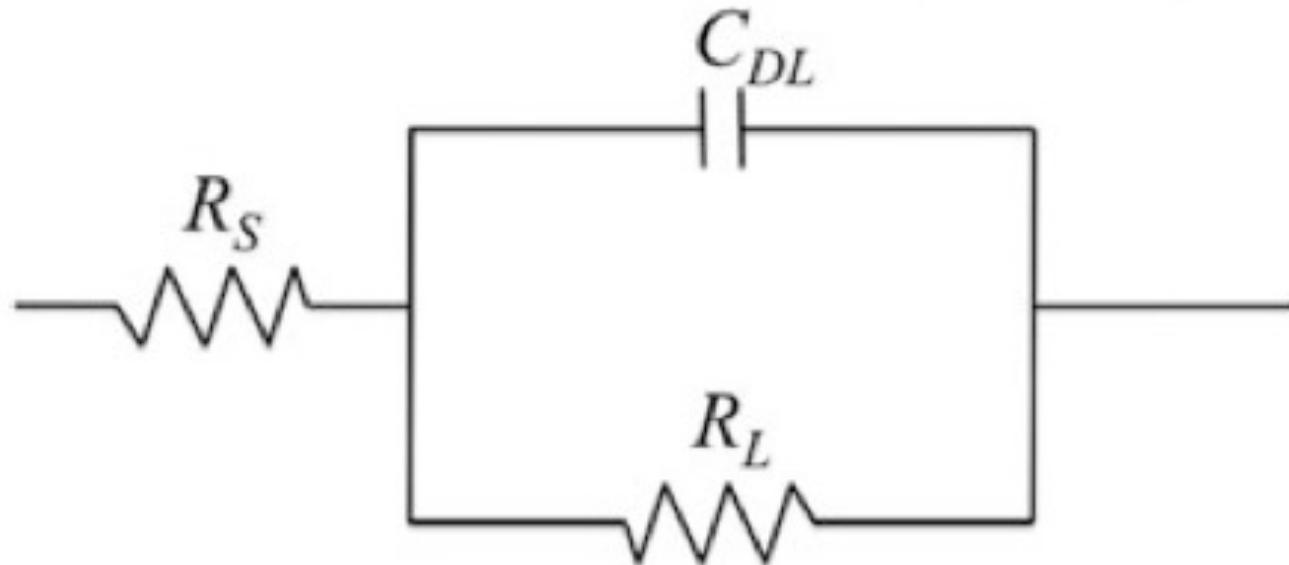
DNA specific detection by immobilizing
the right ssDNA sequence

Impedimetric Sensing



Clearly, the impedance of the Bio/CMOS interface changes accordingly to molecular steric hindrance

Equivalent Impedance



Randles model for the Layering effects

Equivalent Impedance

$$Z = \frac{R_L}{j\omega C_{DL}R_L + 1} \cdot \frac{1 - j\omega C_{DL}R_L}{1 - j\omega C_{DL}R_L}$$

$$Z = \frac{R_L - j\omega C_{DL}R_L^2}{1 + (\omega C_{DL}R_L)^2}$$

$$Z = \frac{R_L}{1 + (\omega C_{DL}R_L)^2} - j \frac{\omega C_{DL}R_L^2}{1 + (\omega C_{DL}R_L)^2} \quad \left\{ \begin{array}{l} Z_{\text{Re}} = \frac{R_L}{1 + (\omega C_{DL}R_L)^2} \\ Z_{\text{Im}} = -\frac{\omega C_{DL}R_L^2}{1 + (\omega C_{DL}R_L)^2} \end{array} \right.$$

This impedance presents both resistive and reactive components

Nyquist Plot



The Nyquist plot is also a mean to fit data about a specific electrochemical cell

Nyquist Plot

$$\underline{Z}_{//} = R_{//} + jX_{//}, \text{ with } \begin{cases} y = -X_{//} = \frac{\omega R_L C_{DL}}{1 + (\omega R_L C_{DL})^2} \\ x = R_{//} = \frac{R_L}{1 + (\omega R_L C_{DL})^2} \end{cases}$$

$$|\underline{Z}_{//}|^2 = \frac{R_L^2 \left[1 + (\omega R_L C_{DL})^2 \right]}{\left[1 + (\omega R_L C_{DL})^2 \right]^2} = \frac{R_L^2}{\left[1 + (\omega R_L C_{DL})^2 \right]} = R_L R_{//}$$

Demonstration that it is a circle
in the Complex plane

Nyquist Plot

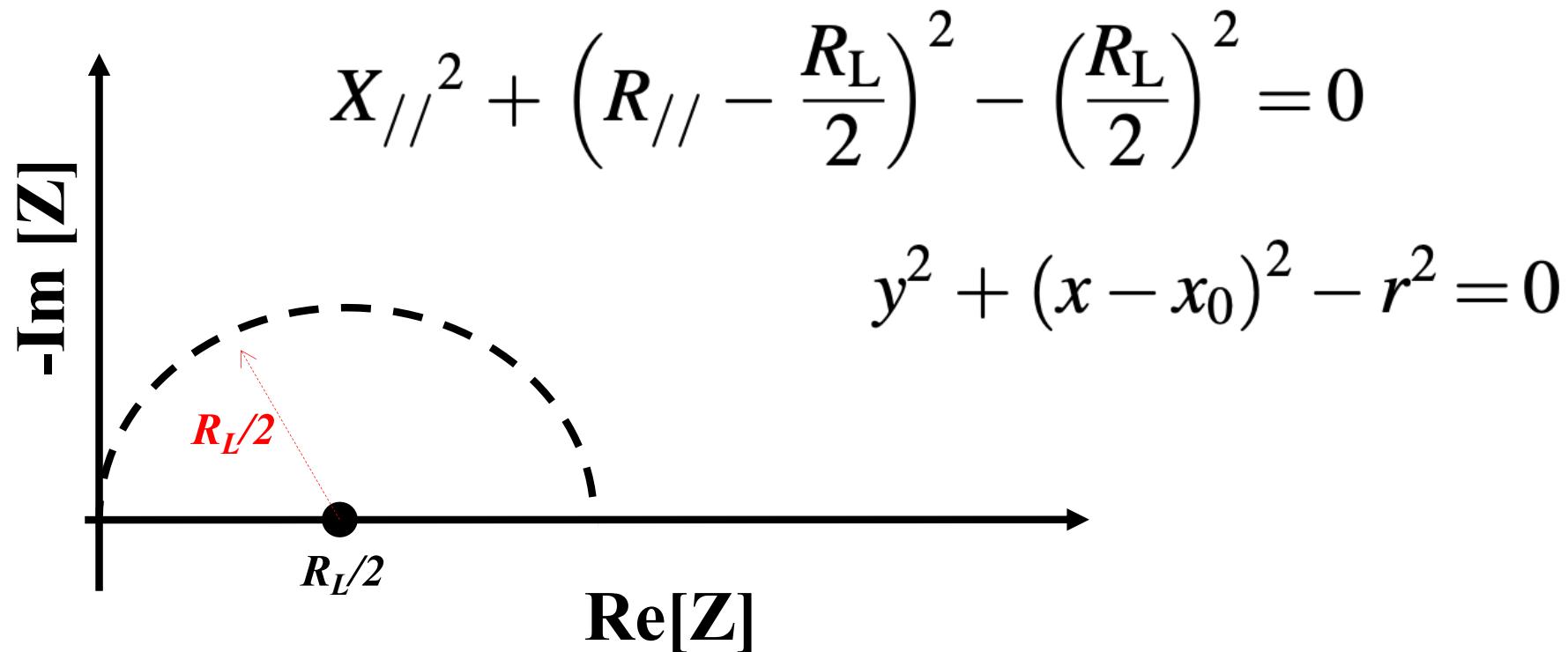
$$Z_{//}^2 = R_{//}^2 + X_{//}^2 = R_L R_{//}$$

$$R_{//}^2 + X_{//}^2 - R_L R_{//} = 0$$

$$X_{//}^2 + \left(R_{//} - \frac{R_L}{2} \right)^2 - \left(\frac{R_L}{2} \right)^2 = 0$$

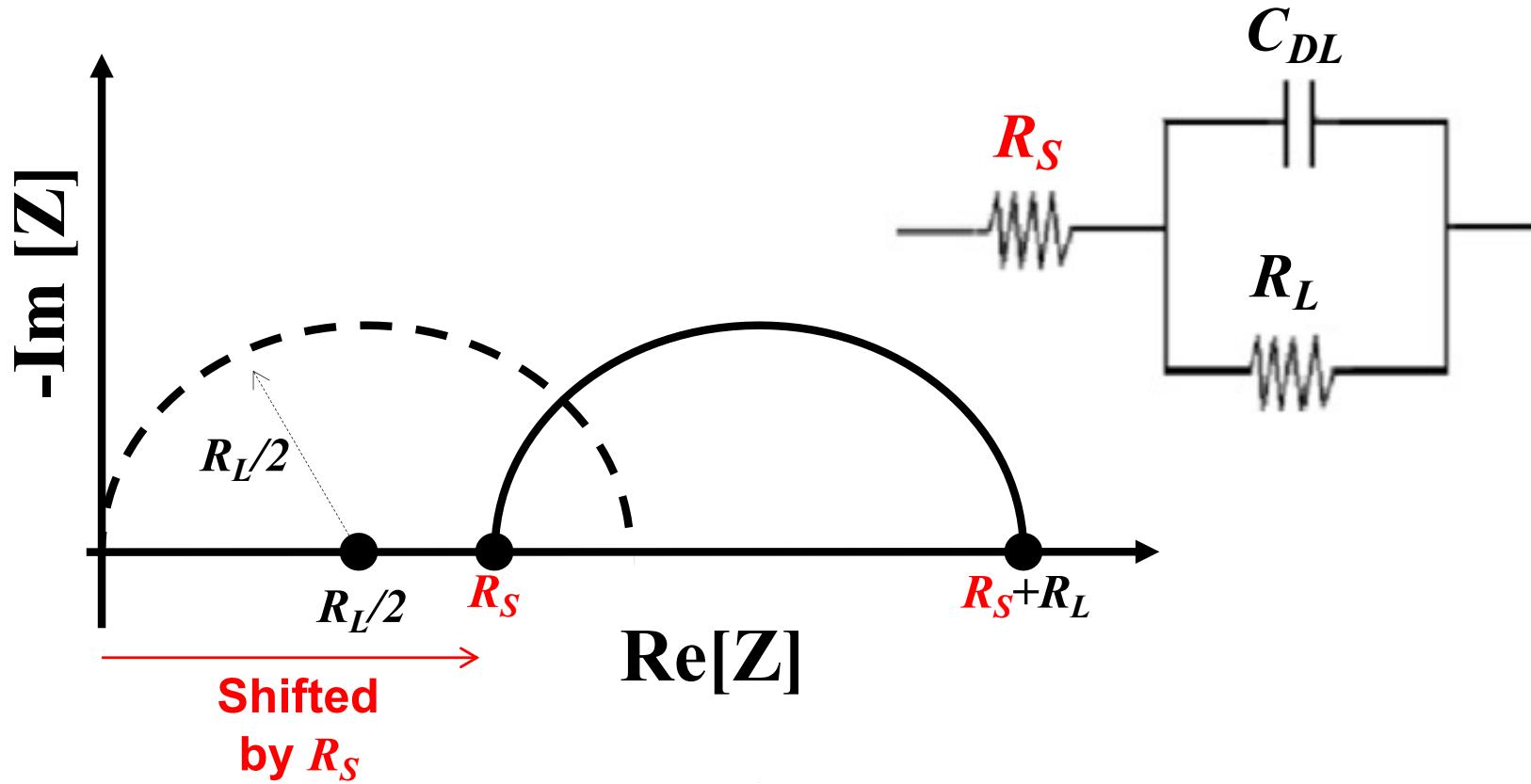
Demonstration that it is a circle
in the Complex plane

Nyquist Plot



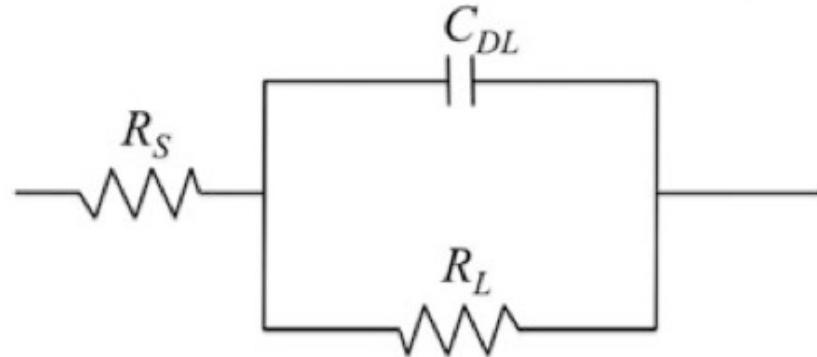
Demonstration that it is a circle
in the Complex plane

Nyquist Plot



That bring us actually to a circle
shifted by R_s in the Complex plane

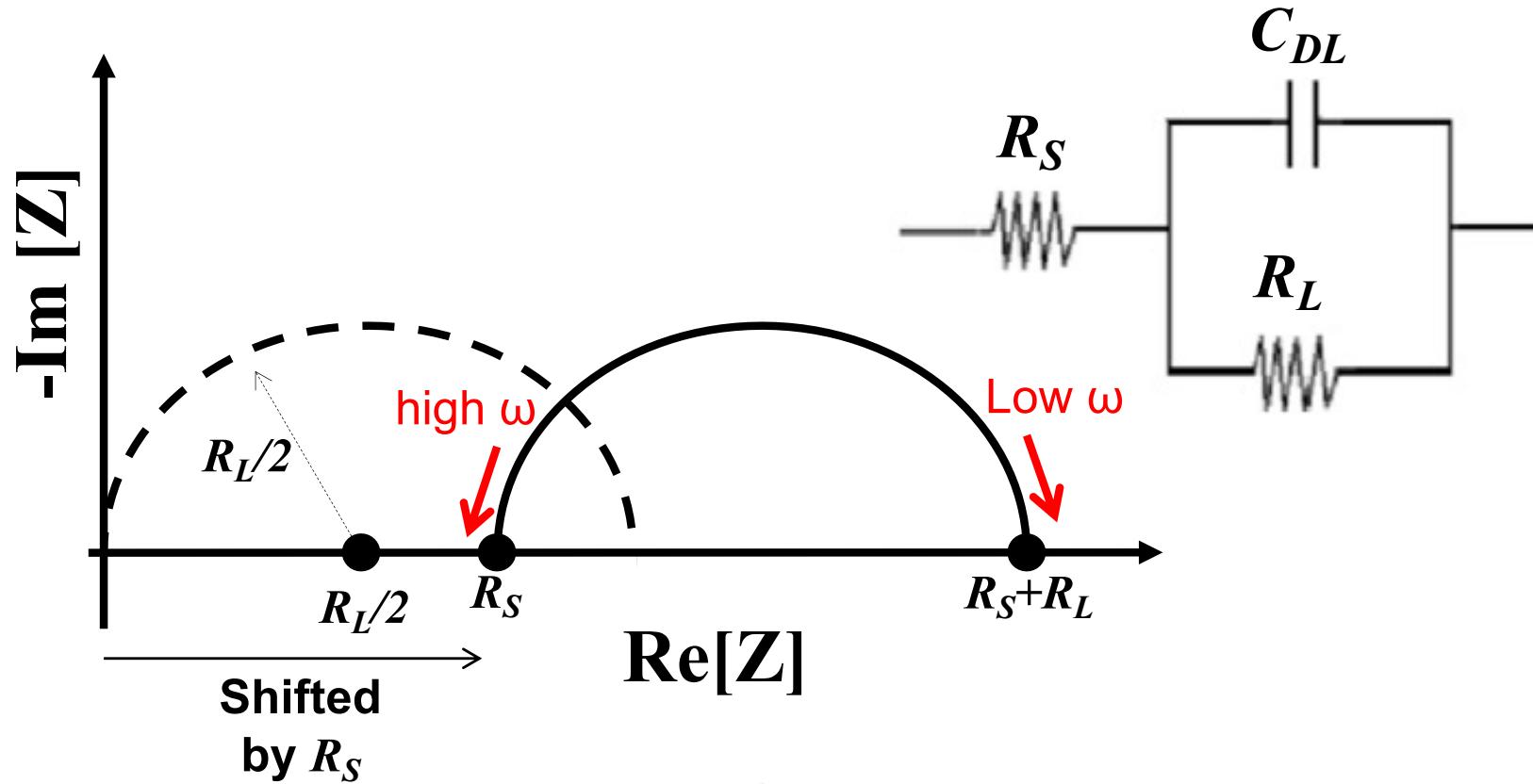
Equivalent Impedance



$$Z_{//} = Z = C_{DL} // R_L \quad \left\{ \begin{array}{l} Z = \frac{R_L}{j\omega C_{DL} R_L + 1} \xrightarrow{\omega \rightarrow 0} R_L \\ Z = \frac{R_L}{j\omega C_{DL} R_L + 1} \xrightarrow{\omega \rightarrow \infty} 0 \end{array} \right.$$

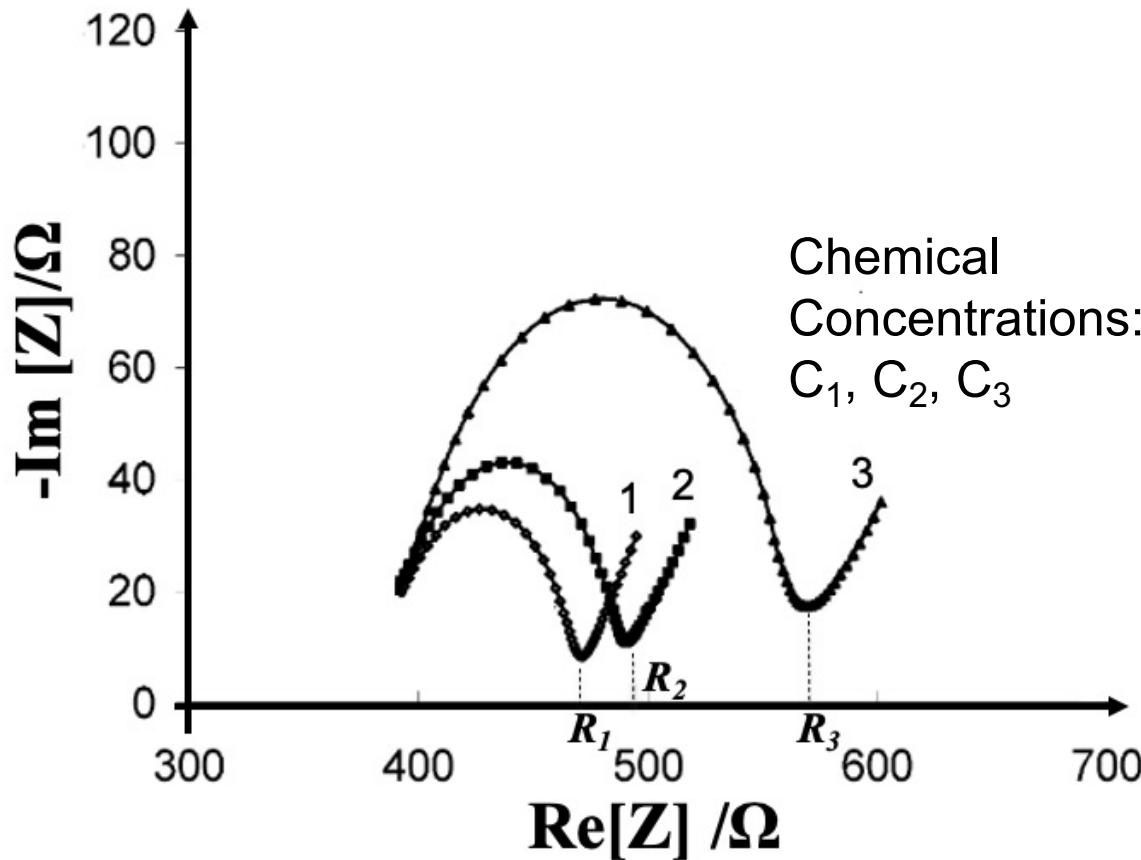
Frequency drive the move on the circle

Nyquist Plot



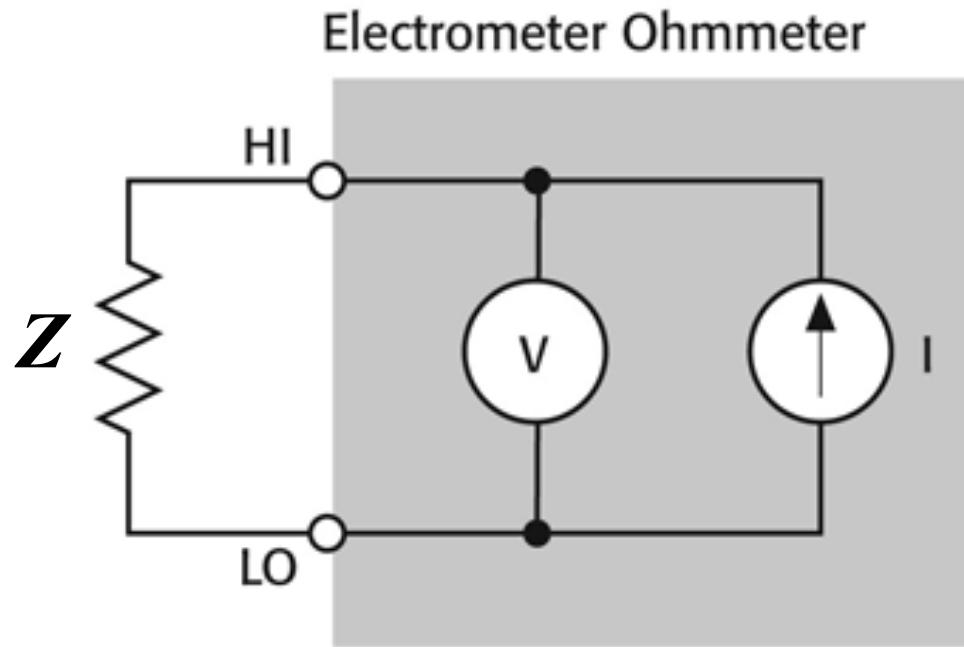
That bring us actually to a circle
shifted by R_s in the Complex plane

Impedimetric Sensing



Nyquist Plots may be used for Molecular Detection by following changes in Z

Impedimetric Sensing

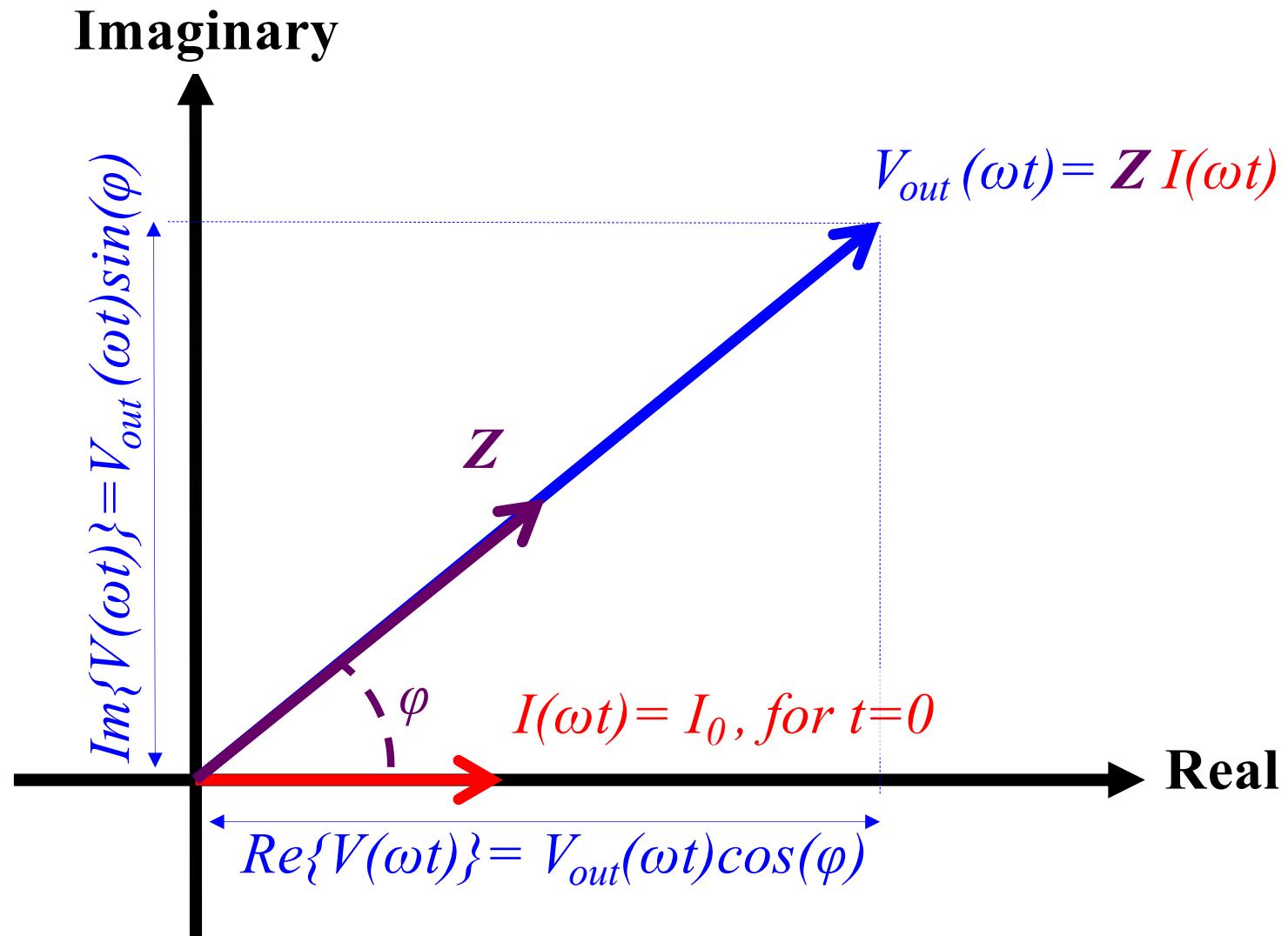


$$\underline{Z} = |Z| e^{j\varphi} = Z[\cos(\varphi) + j \sin(\varphi)]$$

$$I(t) = I_0 \sin(\omega t)$$

$$V_{\text{out}} = \underline{Z}I(t) = ZI_0 \sin(\omega t + \varphi)$$

Impedimetric Sensing



Impedimetric Sensing

$$V_{\text{out}} = \underline{ZI}(t) = ZI_0 \sin(\omega t + \varphi)$$

$$\begin{cases} \text{Re}\{\underline{V}_{\text{out}}(\omega t)\} = \underline{V}_{\text{out}}(\omega t) \cos(\varphi) \\ \text{Im}\{\underline{V}_{\text{out}}(\omega t)\} = \underline{V}_{\text{out}}(\omega t) \sin(\varphi) \end{cases}$$

$$\text{Re}\{V_{\text{out}}\} = ZI_0 \int_0^T \sin(\omega t + \varphi) \sin(\omega t) dt$$

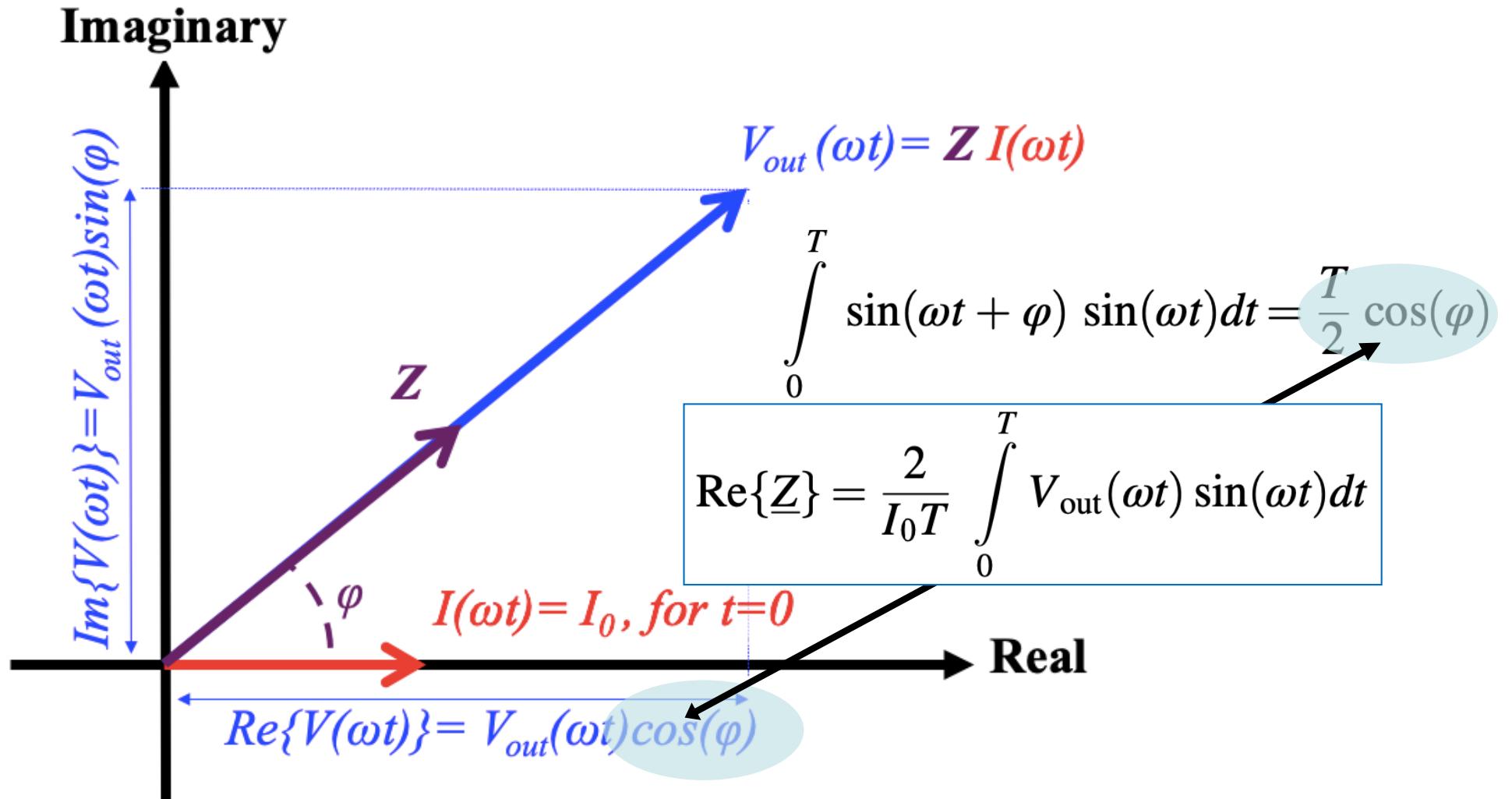
Impedimetric Sensing

$$\operatorname{Re}\{V_{\text{out}}\} = ZI_0 \int_0^T \sin(\omega t + \varphi) \sin(\omega t) dt$$
$$\left\{ \begin{array}{l} \sin(\alpha) \cos(\beta) = \frac{1}{2} [\sin(\alpha - \beta) + \sin(\alpha + \beta)] = \\ \sin(\alpha) \sin(\beta) = \frac{1}{2} [\cos(\alpha - \beta) - \cos(\alpha + \beta)] = \\ \cos(\alpha) \cos(\beta) = \frac{1}{2} [\cos(\alpha - \beta) + \cos(\alpha + \beta)] \end{array} \right.$$

$$\int_0^T \sin(\omega t + \varphi) \sin(\omega t) dt = \frac{1}{2} \left[\int_0^T \cos(\varphi) dt - \int_0^T \cos(2\omega t + \varphi) dt \right]$$

$$\int_0^T \sin(\omega t + \varphi) \sin(\omega t) dt = \frac{T}{2} \cos(\varphi)$$

Impedimetric Sensing



Impedimetric Sensing

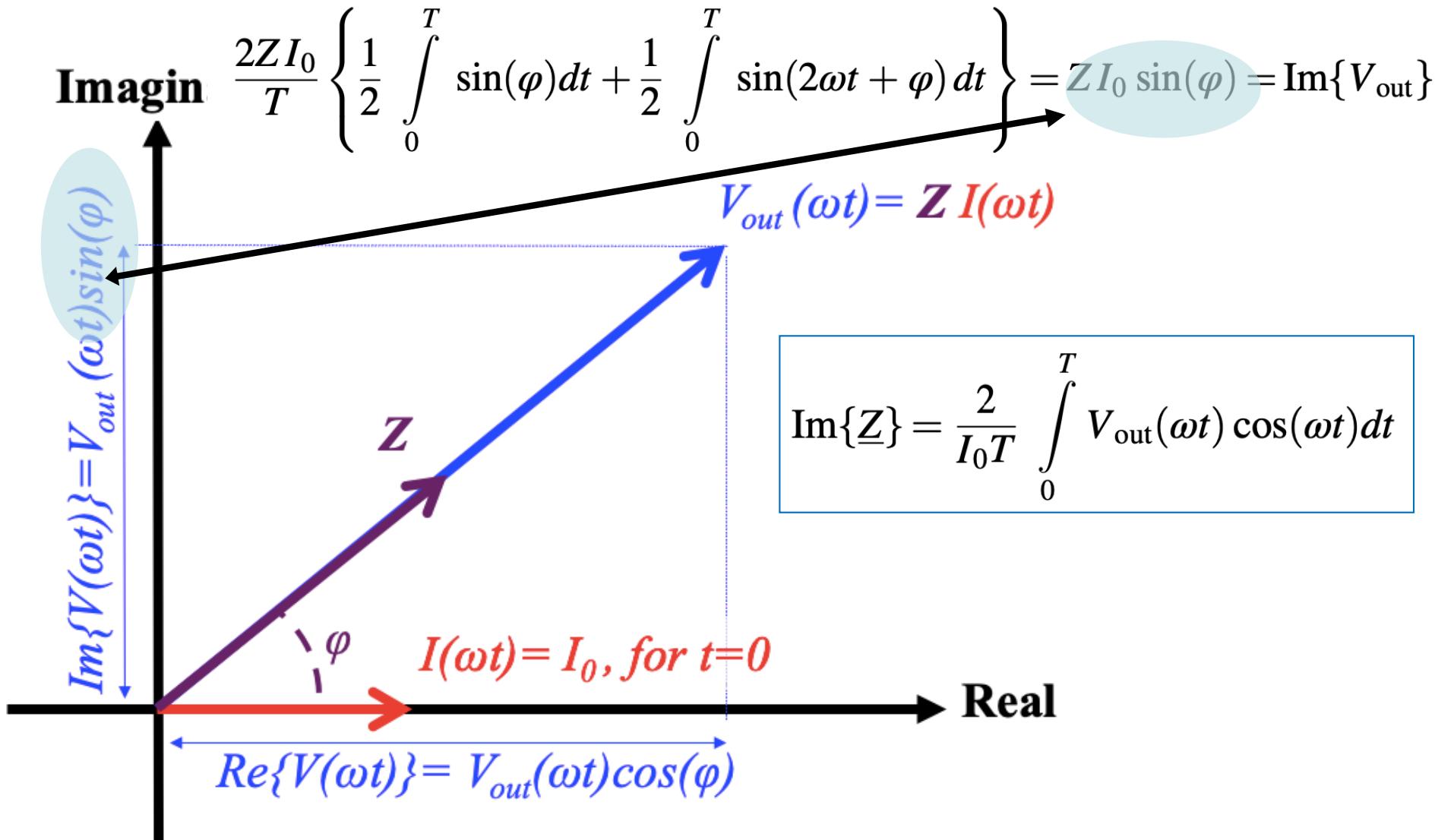
$$\text{Im}\{V_{\text{out}}\} = \frac{2ZI_0}{T} \int_0^T \sin(\omega t + \varphi) \cos(\omega t) dt$$

$$\left\{ \begin{array}{l} \sin(\alpha) \cos(\beta) = \frac{1}{2} [\sin(\alpha - \beta) + \sin(\alpha + \beta)] = \\ \sin(\alpha) \sin(\beta) = \frac{1}{2} [\cos(\alpha - \beta) - \cos(\alpha + \beta)] = \\ \cos(\alpha) \cos(\beta) = \frac{1}{2} [\cos(\alpha - \beta) + \cos(\alpha + \beta)] = \end{array} \right.$$

$$\frac{2ZI_0}{T} \left\{ \frac{1}{2} \int_0^T \sin(\varphi) dt + \frac{1}{2} \int_0^T \sin(2\omega t + \varphi) dt \right\} = ZI_0 \sin(\varphi) = \text{Im}\{V_{\text{out}}\}$$

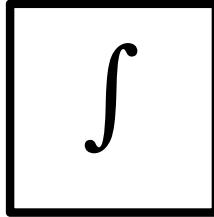
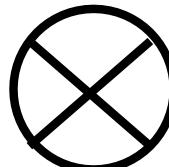
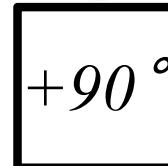
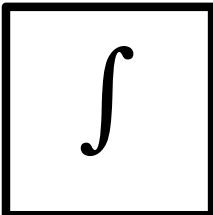
$$\text{Im}\{\underline{Z}\} = \frac{2}{I_0 T} \int_0^T V_{\text{out}}(\omega t) \cos(\omega t) dt$$

Impedimetric Sensing

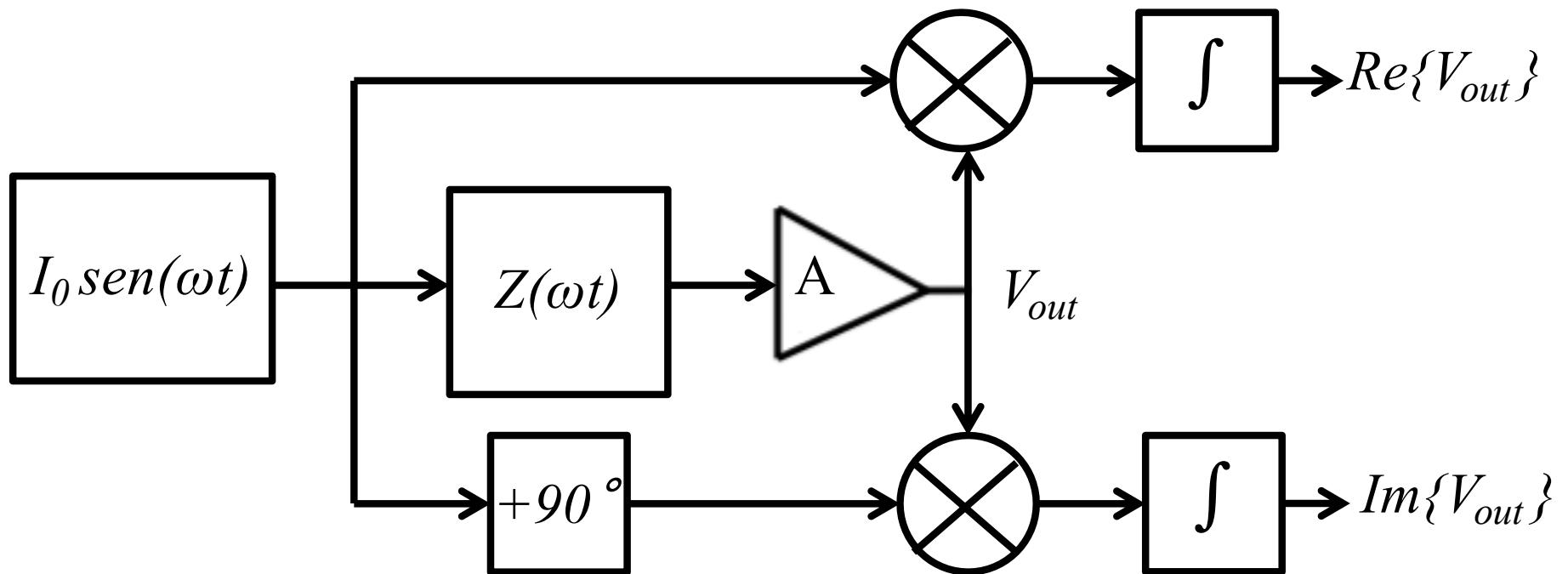


Impedimetric Sensing

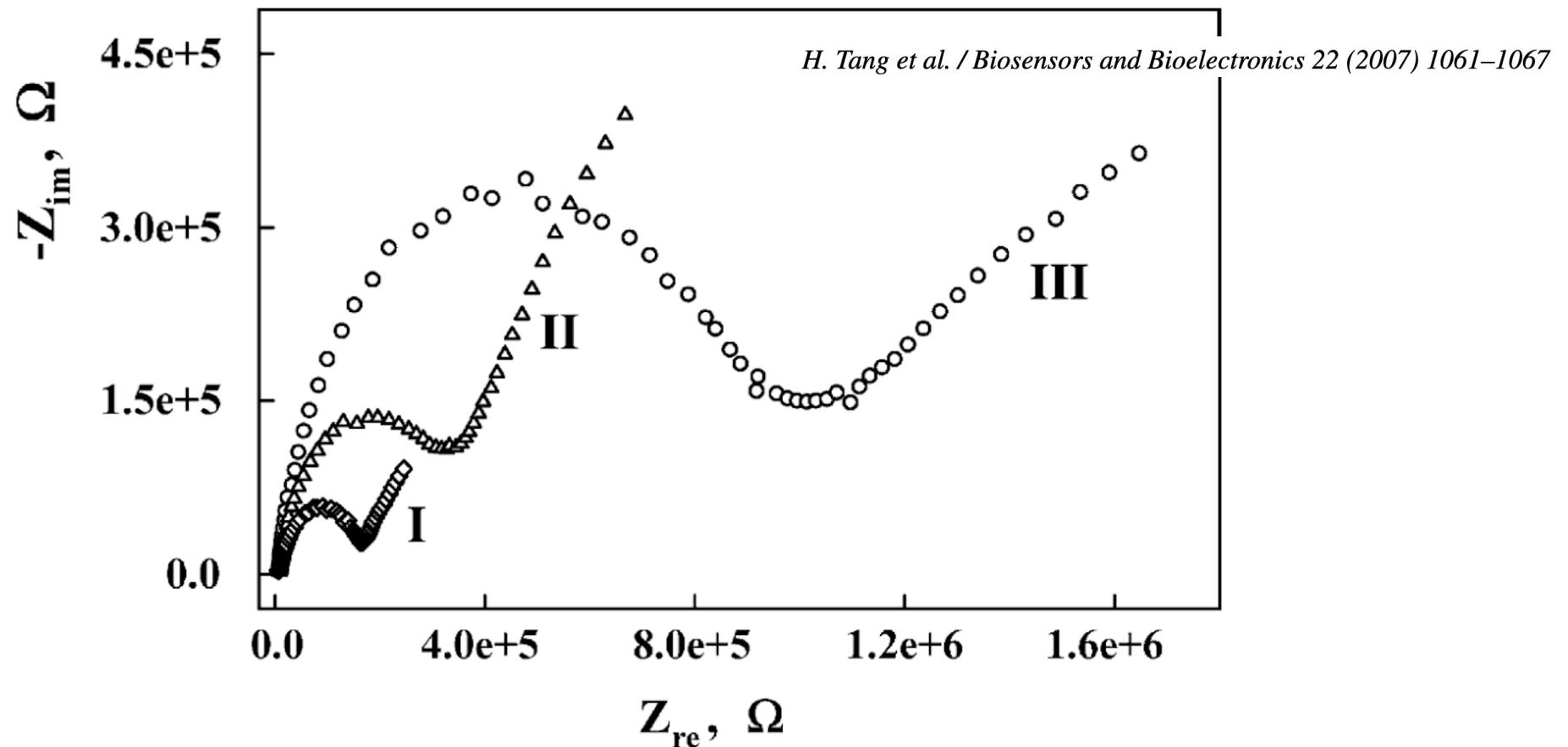
$$\left\{ \begin{array}{l} \text{Re}\{\underline{Z}\} = \frac{2}{I_0 T} \int_0^T V_{\text{out}}(\omega t) \sin(\omega t) dt \\ \text{Im}\{\underline{Z}\} = \frac{2}{I_0 T} \int_0^T V_{\text{out}}(\omega t) \cos(\omega t) dt \end{array} \right.$$

Impedimetric Sensing

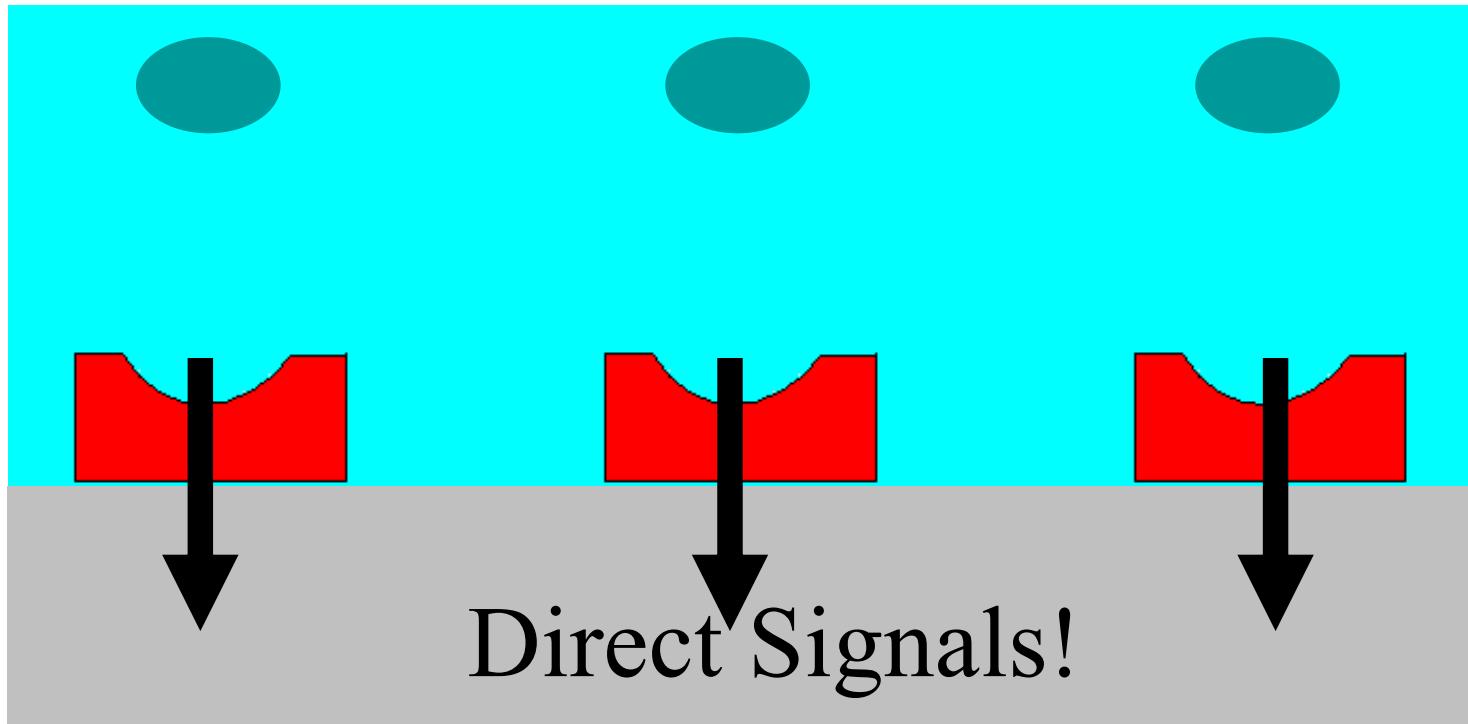


Impedimetric Sensing of CEA



Nyquist plots: I-bare ; II-Antibodies ; and III-uptake with CEA (CarcinoEmbryonic Antigen)

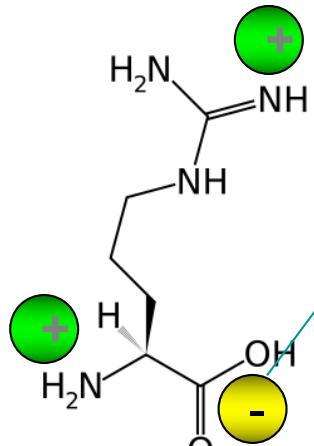
CMOS/Sample interface



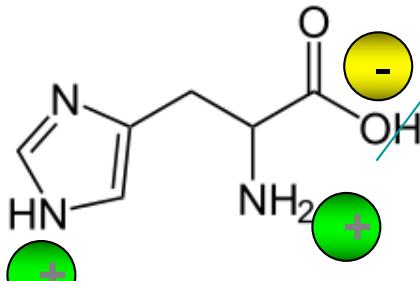
How to get direct signals of probe/target interactions in case of antibodies or ssDNA probes?

Charged Residues

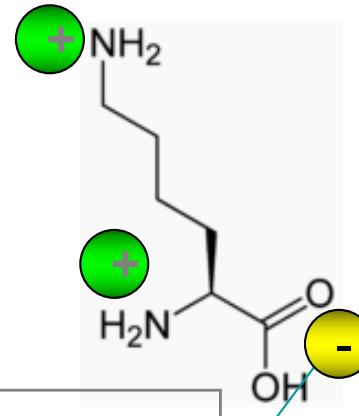
Positively Charged



Arginine

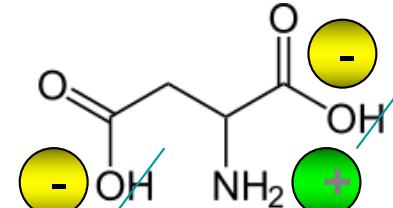


Histidine

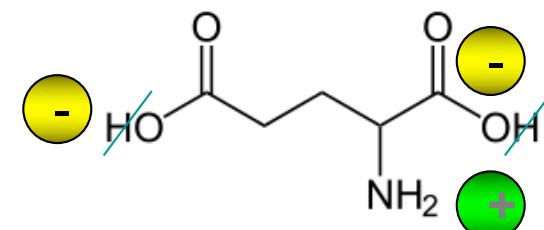


Lysine

Neg. Charged

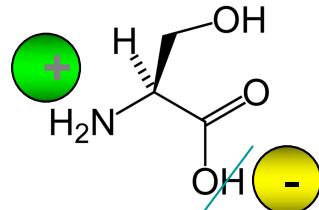


Aspartic Acid

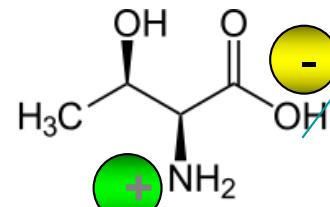


Glutamic Acid

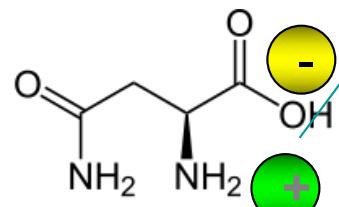
Polar Uncharged



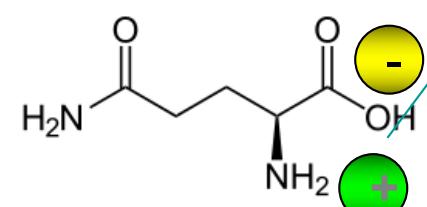
Serine



Threonine



Asparagine



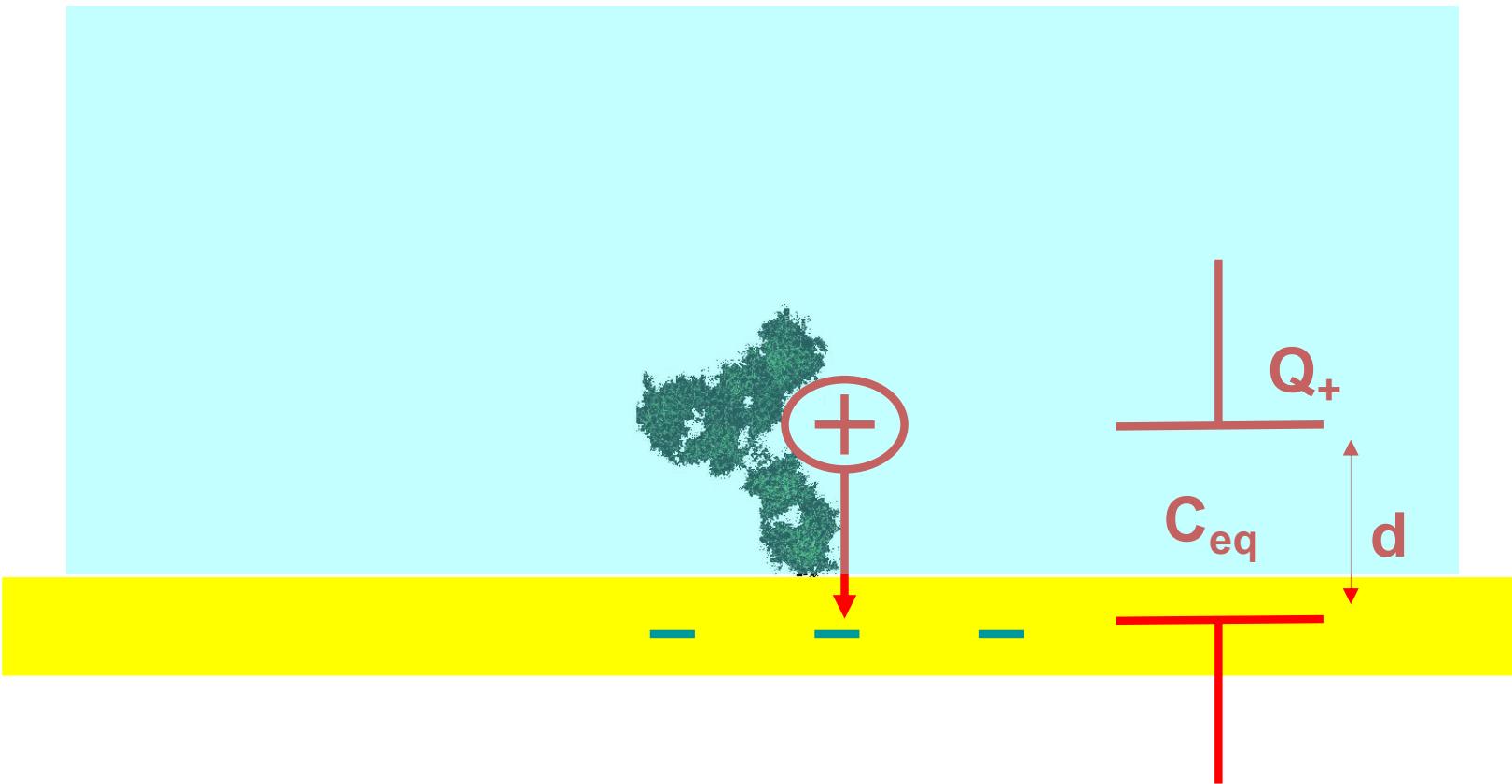
Glutamine

The charges of an Antibody



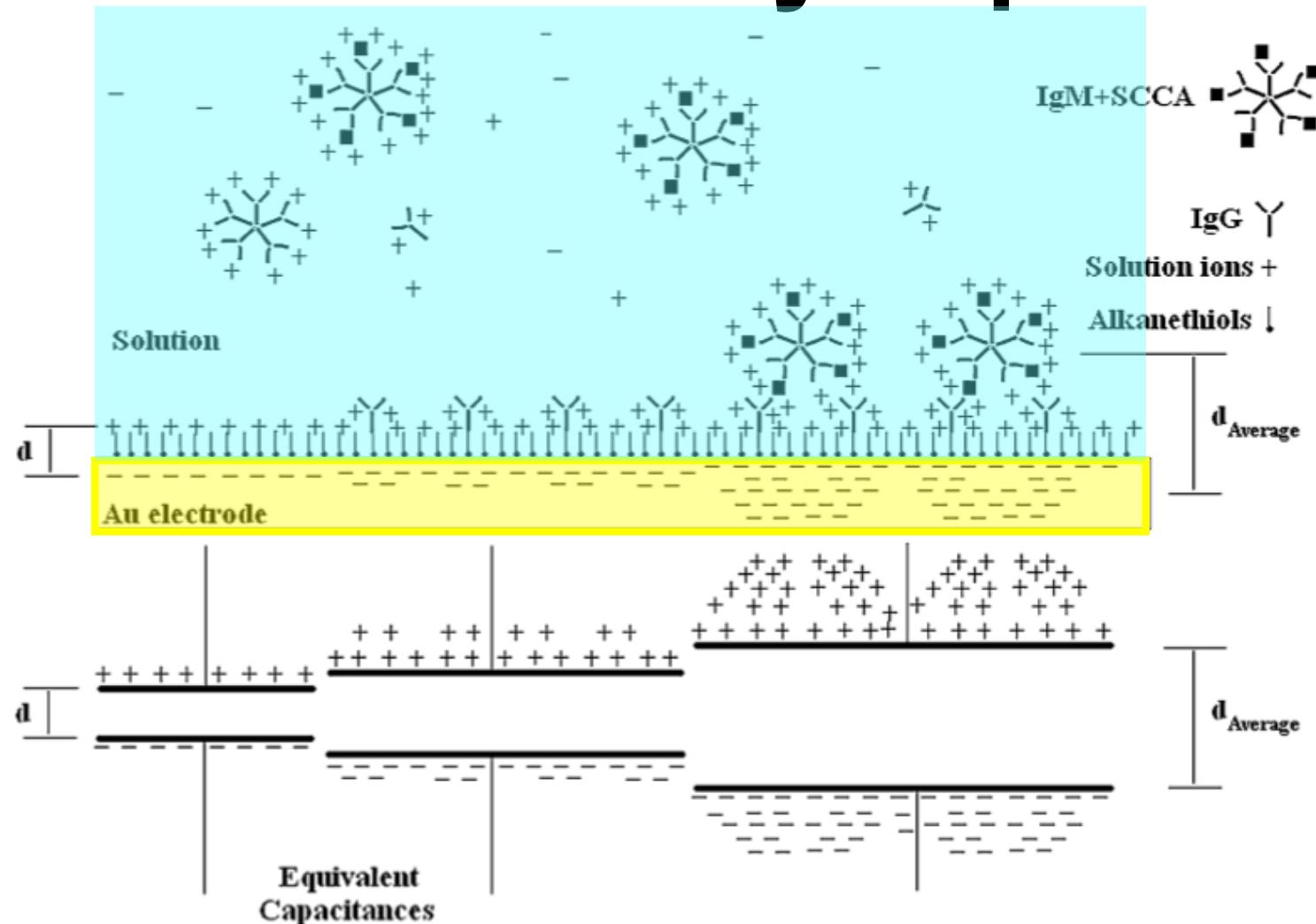
The crystallographic structure of an antibody

Capacitive detection



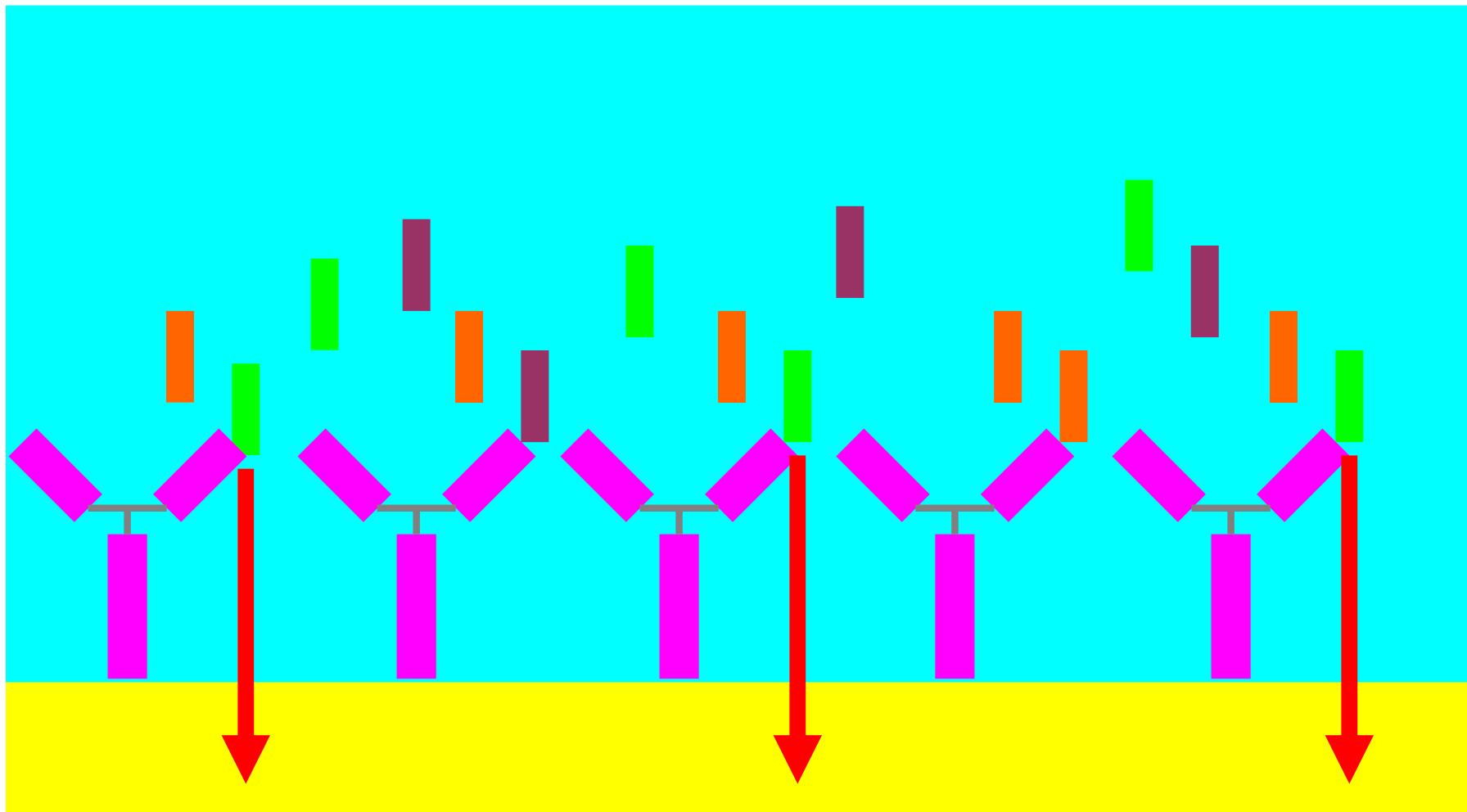
Charged residues of the antibody may affect charge carriers in the electrode

Cancer Detection by capacitance



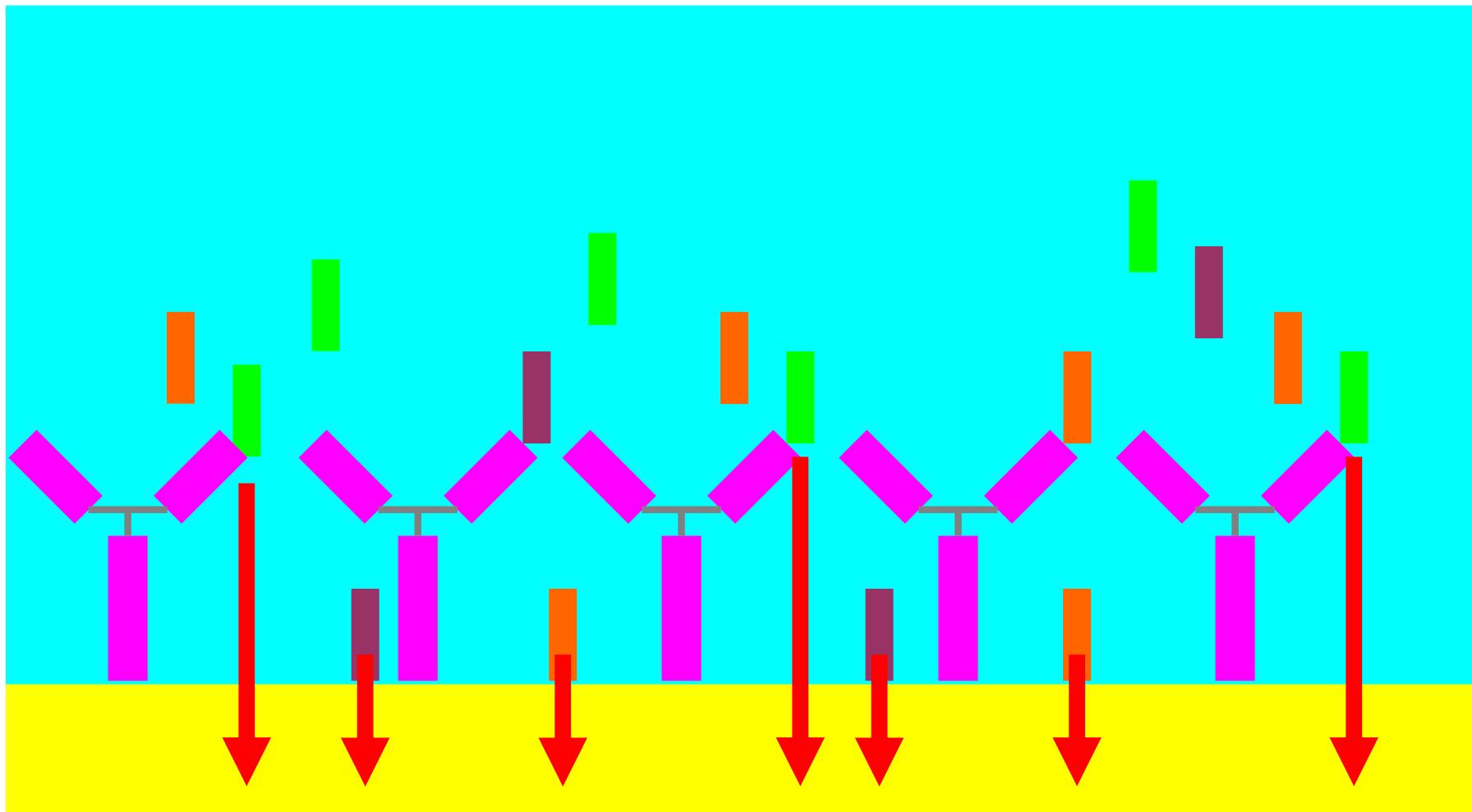
Schematic of the capacitive detection principle

Specificity of the Surface



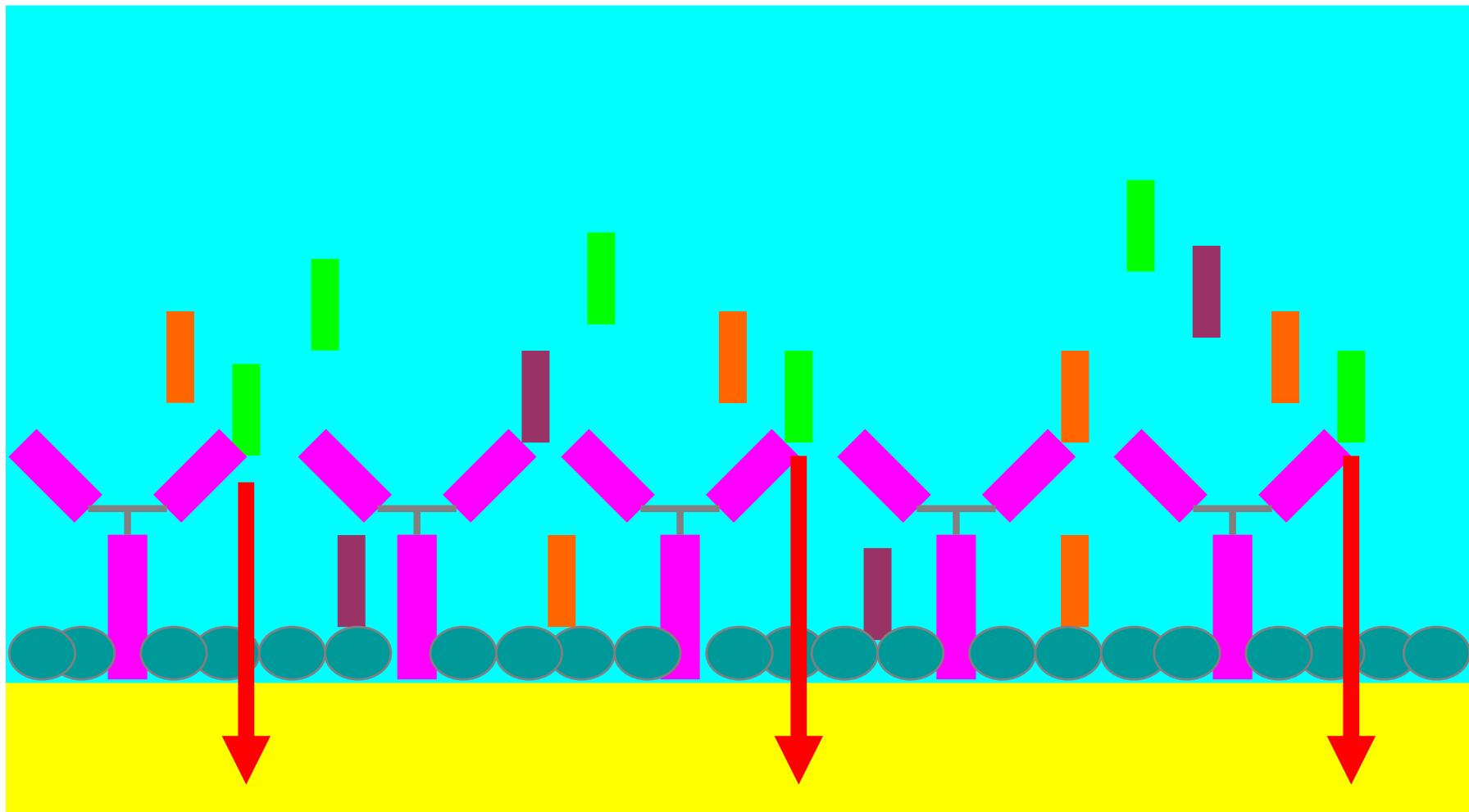
Antigens are specific detected by immobilizing the right antibodies

Specificity of the Surface



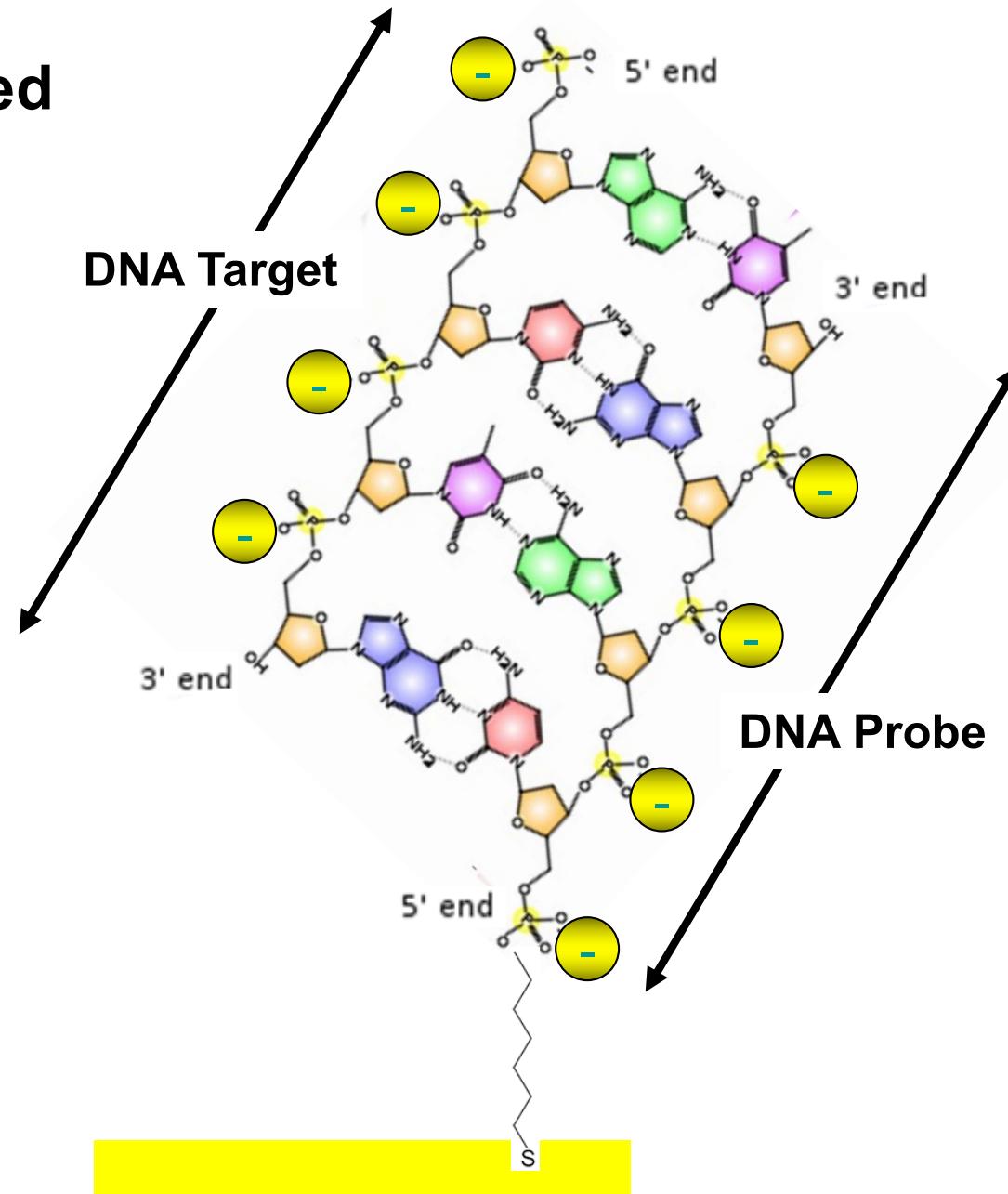
Antibodies are specific but the resulting surface might not be specific enough

Specificity of the Surface



Blocking agents are used
to improve surface specificity

DNA probe and target hybridized on a solid substrate

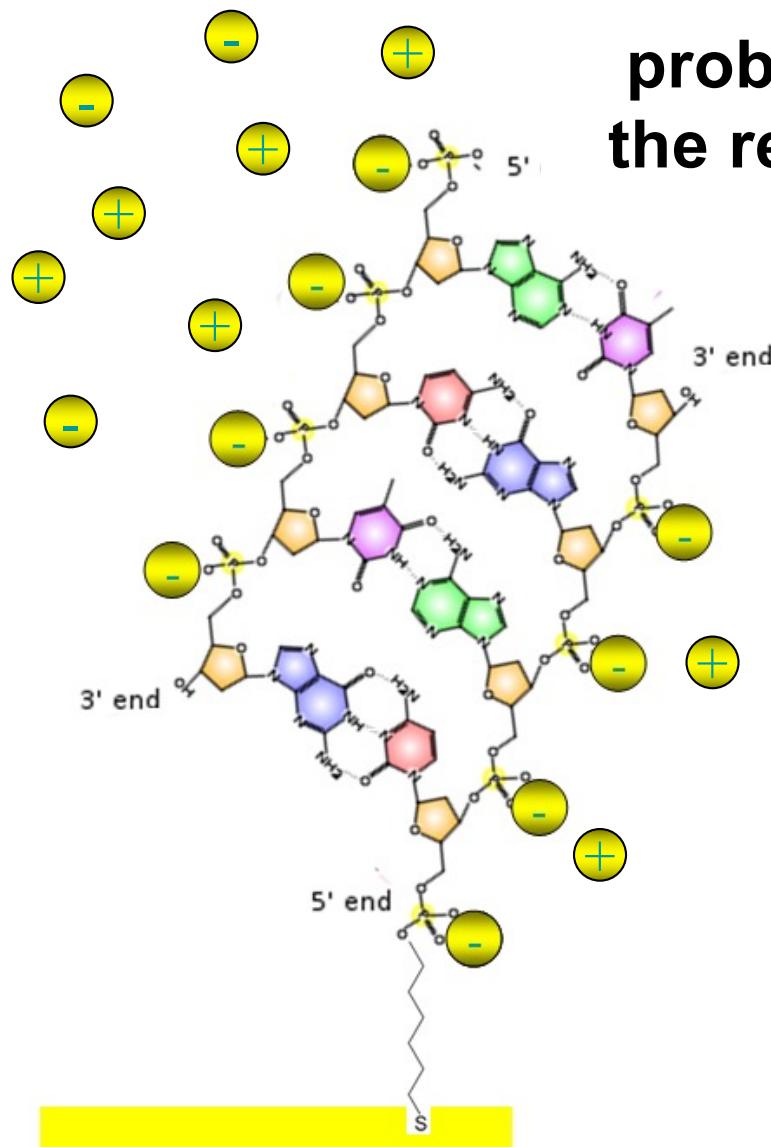


Hybridization degree of DNA

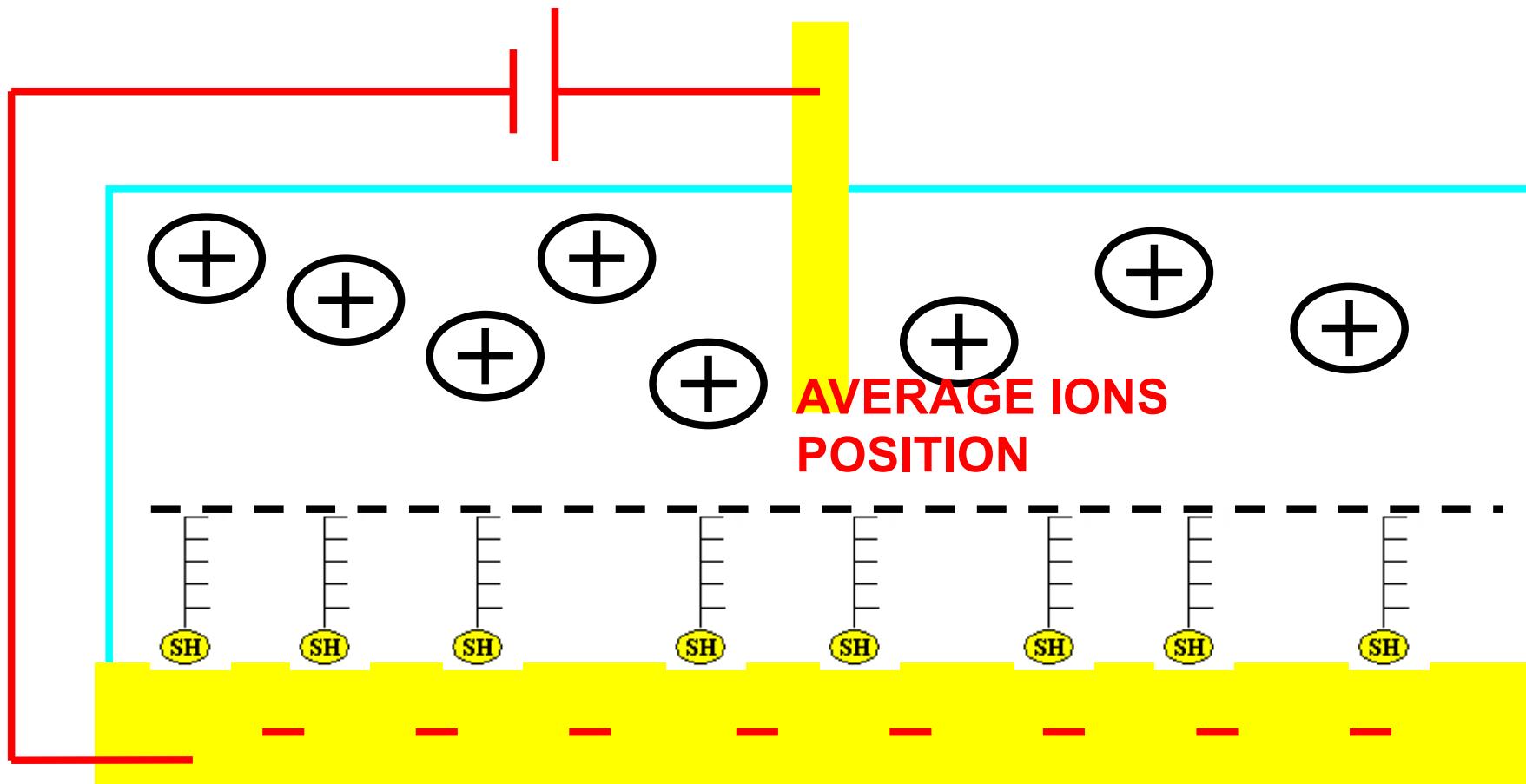
Duplex	ΔG [kJ/mol]
GGTTATTGG CCAATAACC	-26.8
GGTTATTGG CCAAAAAACCC	-12.0
GGTTCTTGG CCAATAACC	-12.4

Gibbs free energies of different matching/nonmatching duplexes

DNA probe and hybridized probe/target on a solid substrate and the related solution ions distributions

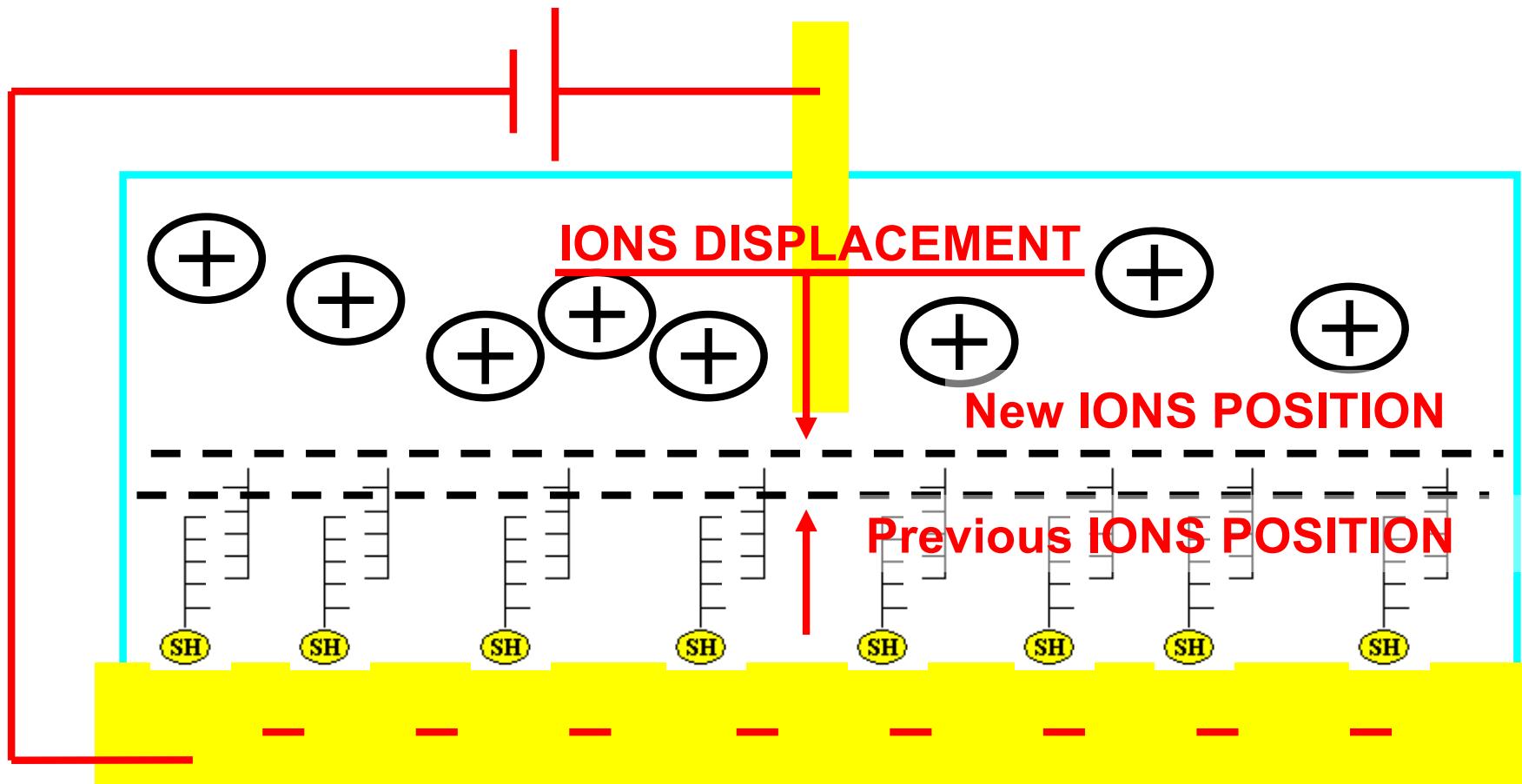


Electrochemical Interface



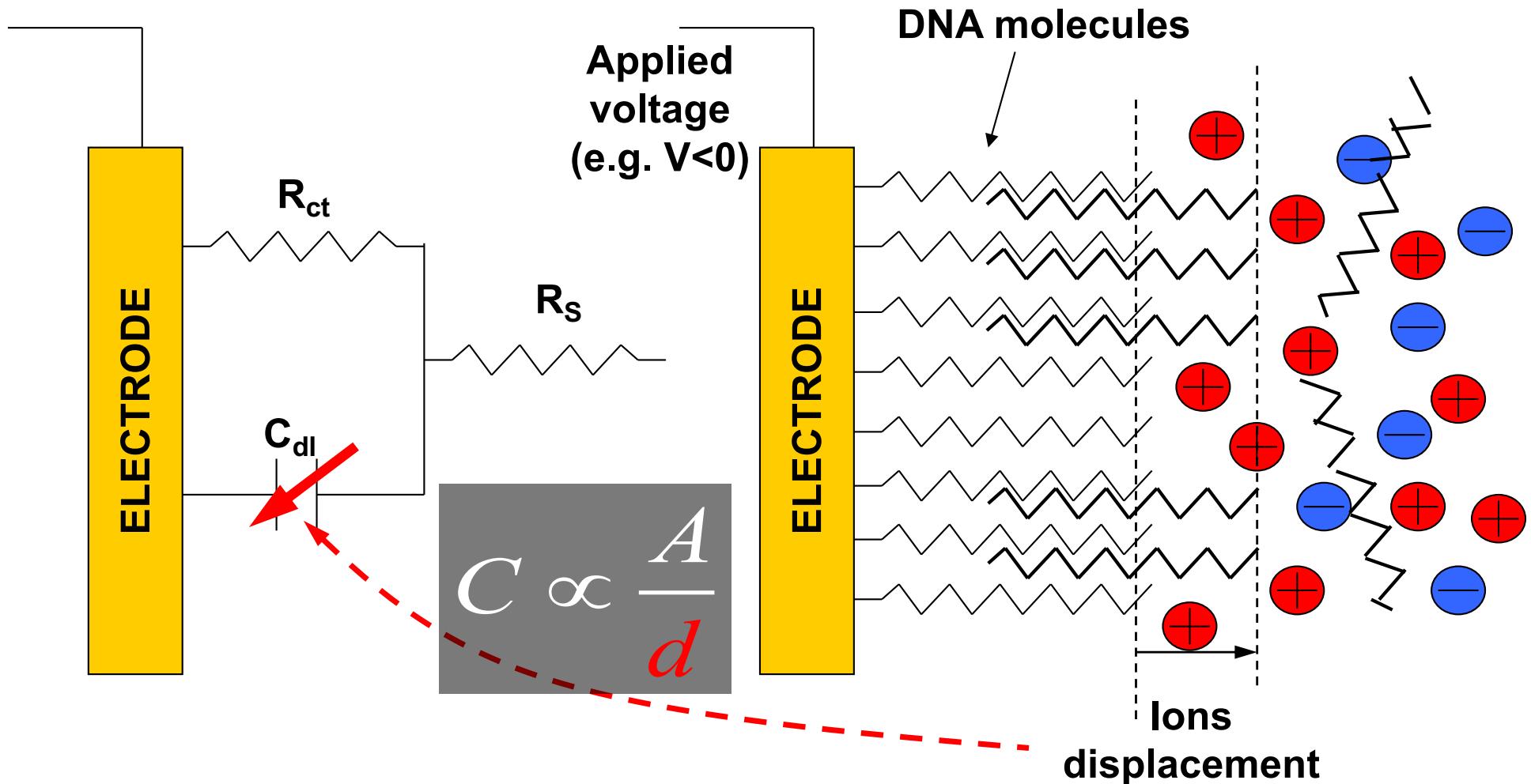
Ion planes are formed at the interface when electrodes immersed in solution are polarized

Electrochemical Interface



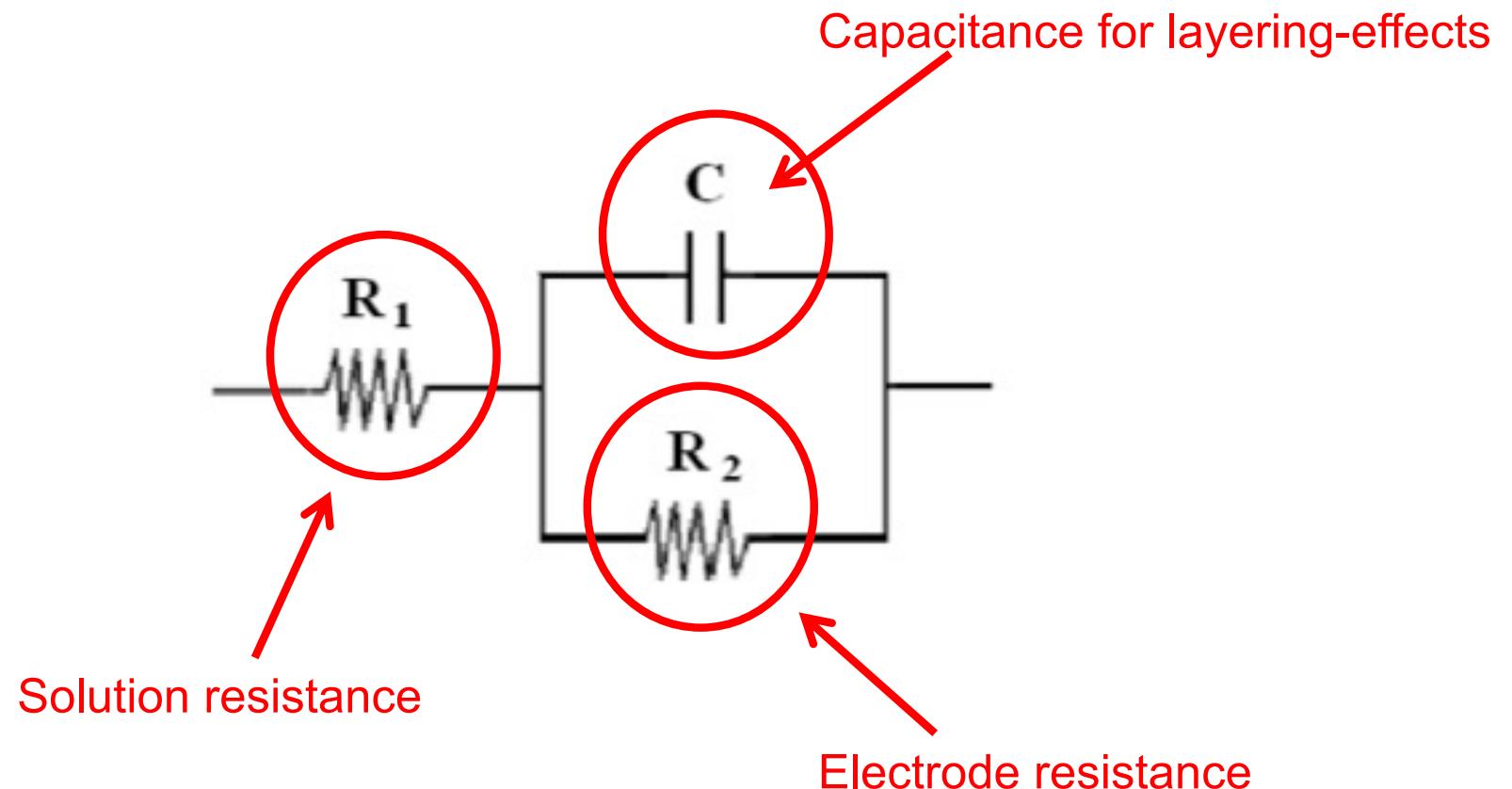
Ion planes are formed at the interface when electrodes immersed in solution are polarized

The Capacitance DNA Detection



Unlabeled ssDNA may be detected with capacitance measurements as due to charge displacement

Equivalent Circuit with Layering effects



Equivalent C of sensing electrodes

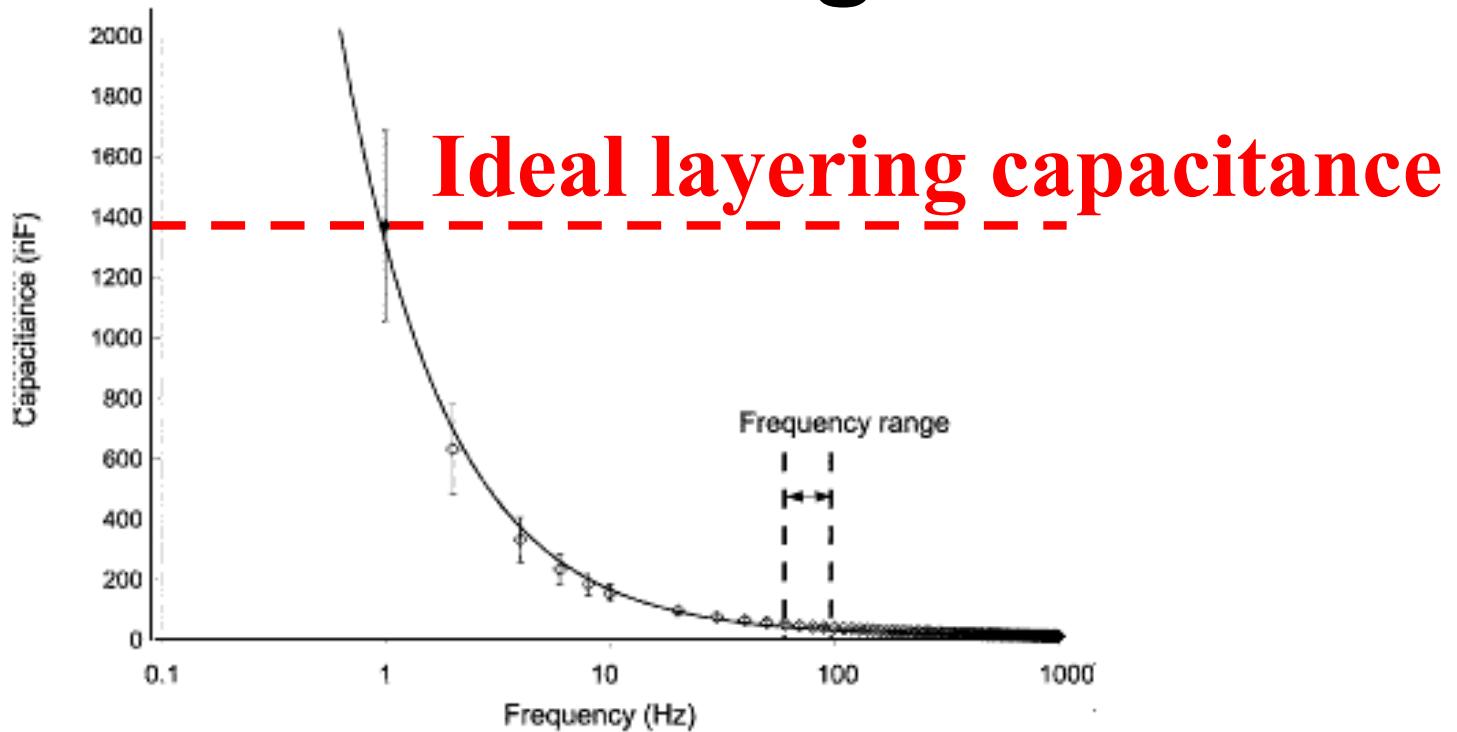
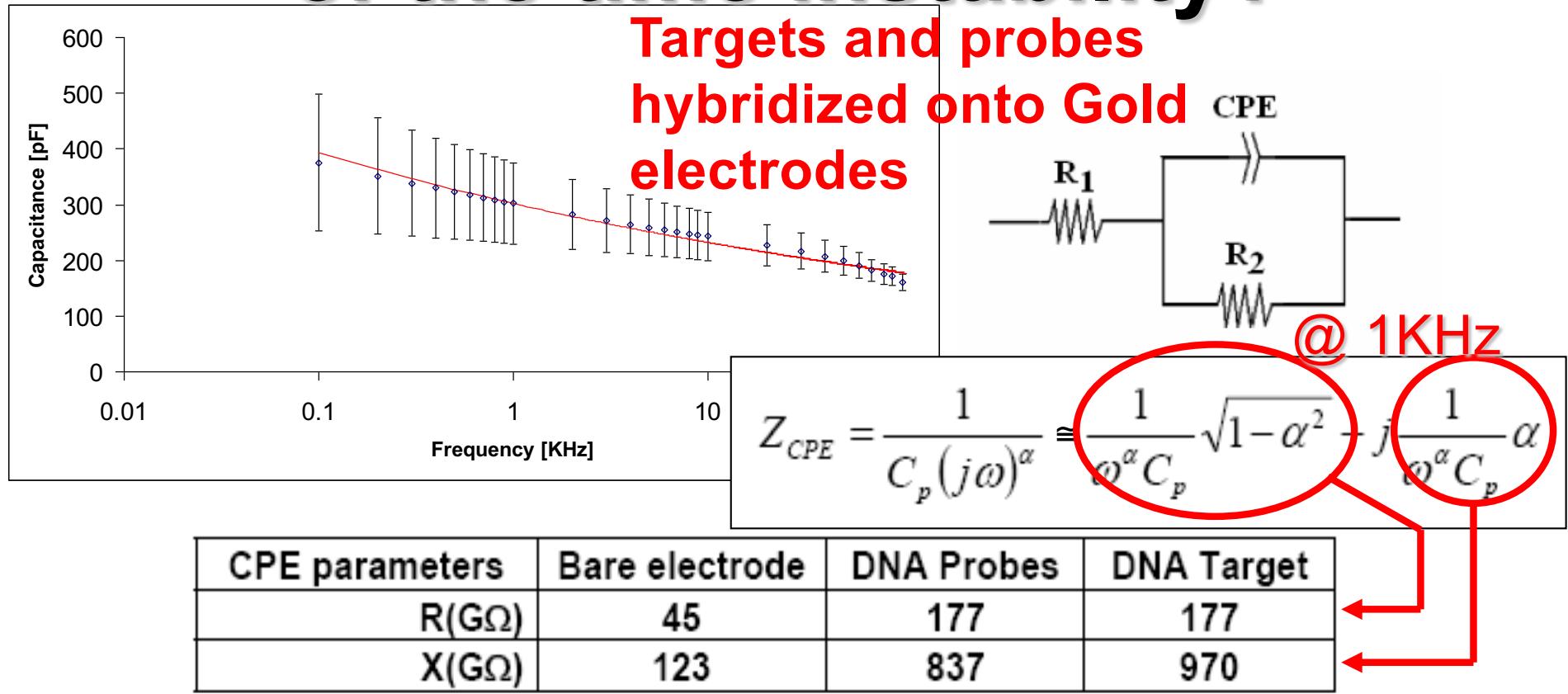


Fig. 9. Measured capacitance versus charge/discharge frequency on clean gold electrodes. The continuous line shows the fitting.

STAGNI *et al.*: FULLY ELECTRONIC LABEL-FREE DNA SENSOR CHIP IEEE SENSORS JOURNAL, VOL. 7, NO. 4, APRIL 2007

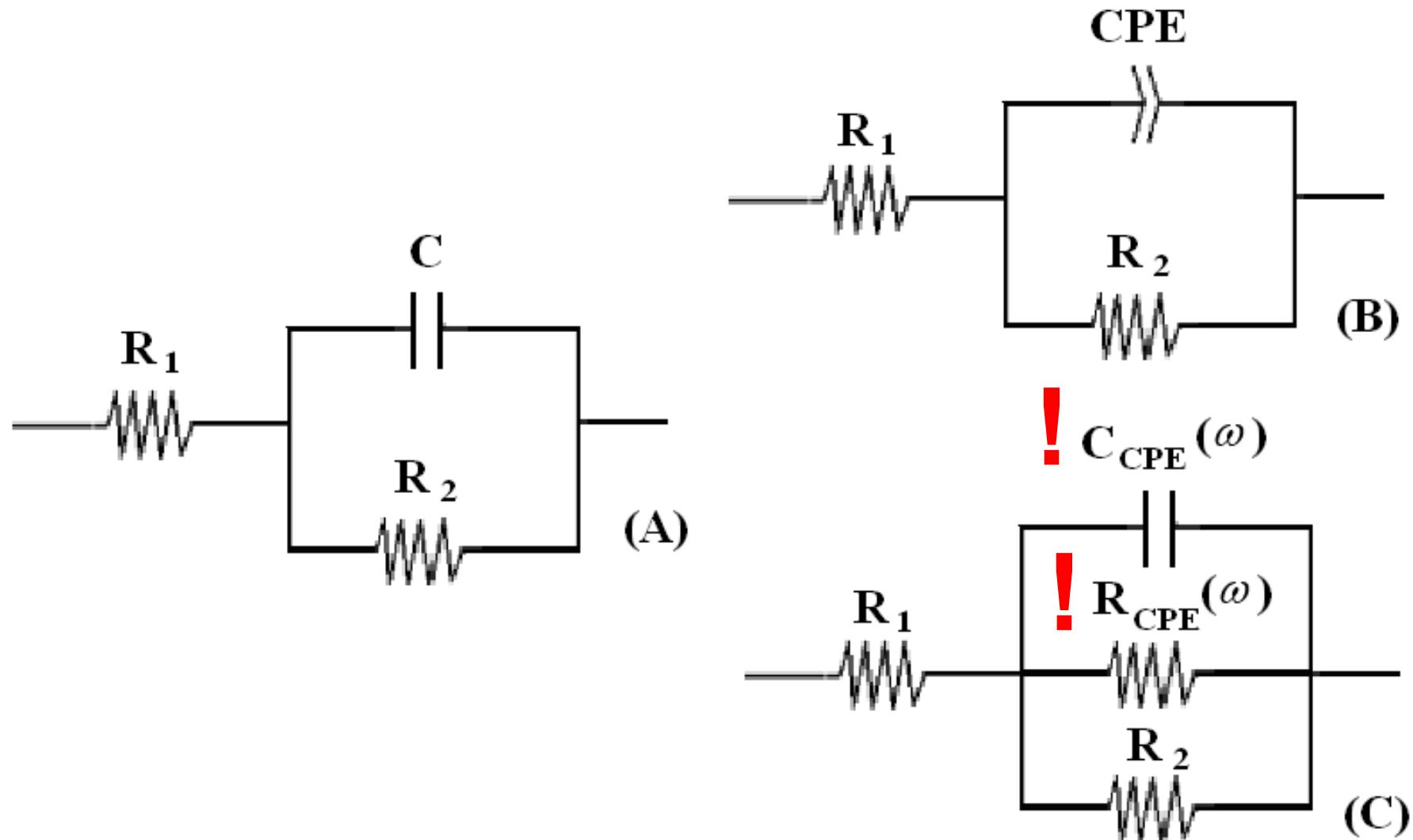
The equivalent capacitance of Helmholtz ion planes on bare electrodes is frequency-dependent

How to understand the reason of the time instability?



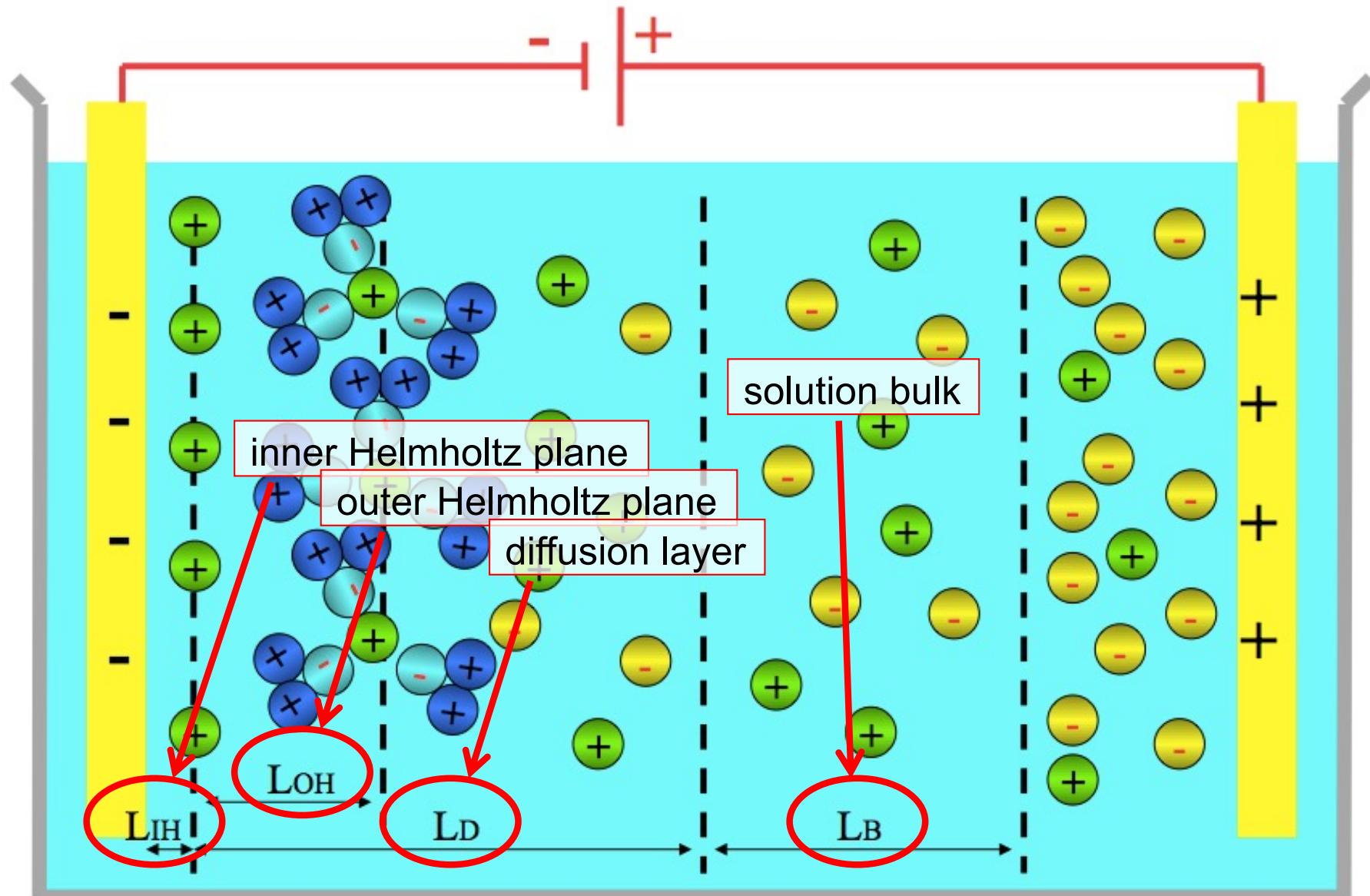
Charge transfer pathways through the DNA layer affect the ideal Capacitance behavior of the interface with the solution sample

Equivalent circuits



Equivalent circuits of DNA Bio/CMOS interface

Helmholtz Planes



Debye Length

Charge density: $\rho_e = \sum_i z_i e n_i$

z_i = charge of species i (e.g. +2, -1, etc.)

n_i = concentration of species i (number per volume)

$$\nabla^2 \phi = 0 \quad \text{In the bulk}$$

$$\nabla^2 \phi = -\frac{\rho_e}{\kappa \epsilon_0} \quad \text{Close to electrodes}$$

For perturbation away from equilibrium at finite temperature

$$\hat{\phi} \equiv \phi - \phi_0 \quad \rho_e = \sum_i z_i e n_{i0} \exp\left(-\frac{z_i e \hat{\phi}}{k_B T}\right)$$

Debye Length

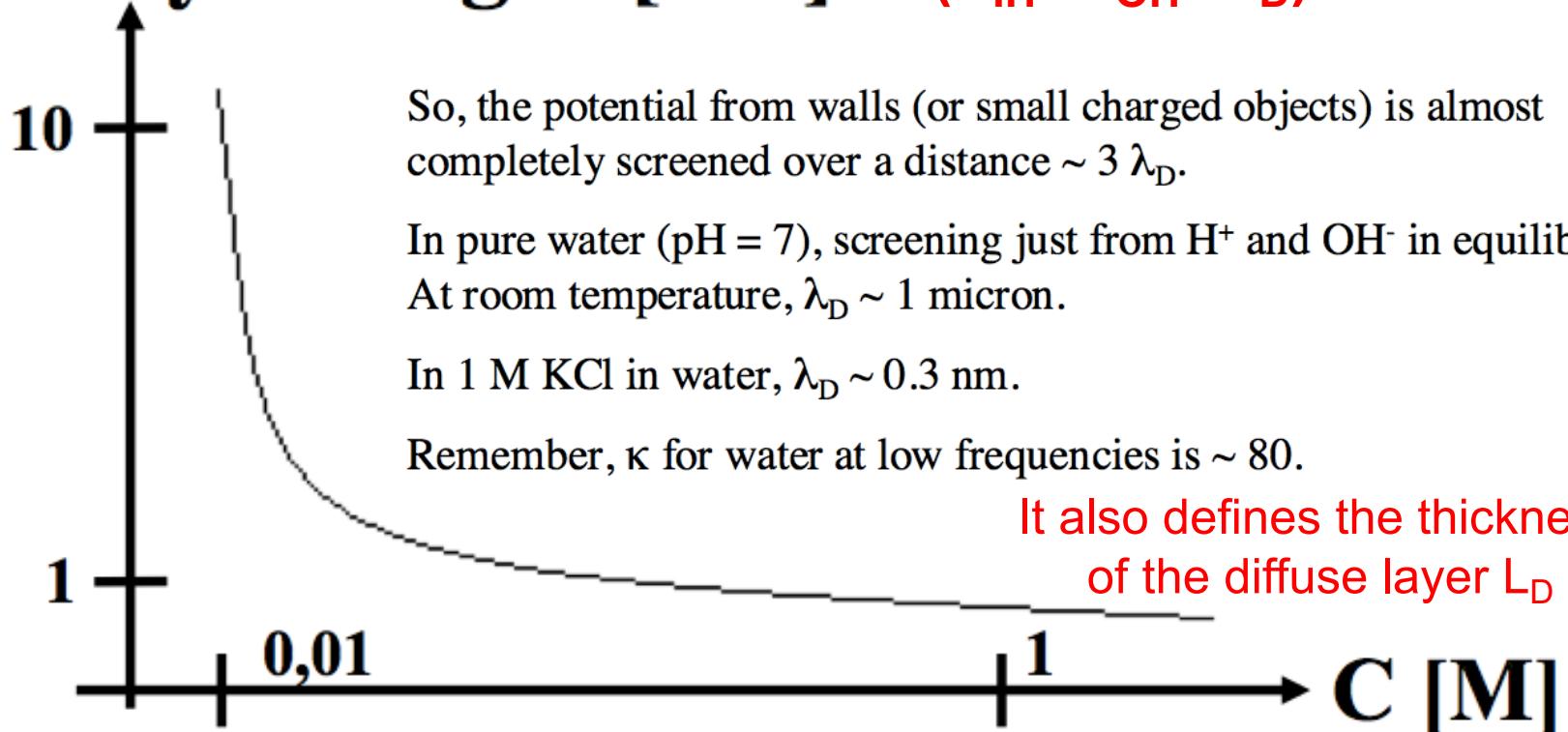
$$\nabla^2 \hat{\phi} = -\frac{1}{\kappa \epsilon_0} \sum_i z_i e n_{i0} \exp\left(-\frac{z_i e \hat{\phi}}{k_B T}\right) \approx -\frac{1}{\kappa \epsilon_0} \sum_i z_i e n_{i0} + \frac{e^2}{\kappa \epsilon_0 k_B T} \sum_i z_i^2 n_{i0} \hat{\phi} \equiv \frac{1}{\lambda_D^2} \hat{\phi}$$

~ 0 for equilibrium neutrality

$$\lambda_D \equiv \left(\frac{e^2}{\kappa \epsilon_0 k_B T} \sum_i z_i^2 n_{i0} \right)^{-1/2}$$

Debye Length

Debye Length [nm] = $(L_{IH} + L_{OH} + L_D)/3$



The Bebye Length is defined as the region of charge carrier's net electrostatic effect in solution

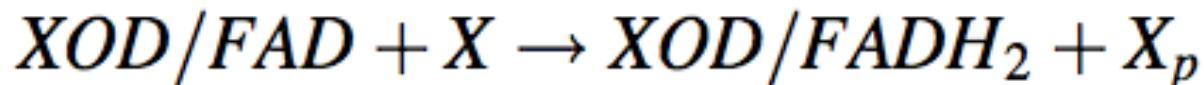
Enzymes' based detection

Some enzymes provide redox reactions in catalysing their substrates. In the case of these enzymes, we can exploit their catalysis for the aim of an electrochemical direct detection.

That's the case of both oxidases and cytochromes.

Redox with oxidases

The typical redox involving an oxidase is as follows:

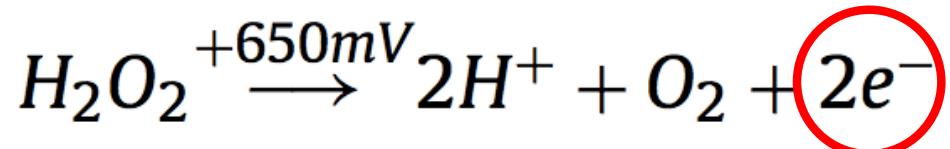


The FAD (Flavin Adenine Dinucleotide) is a functional part of the protein that gains a hydrogen molecule after the reaction. Therefore, the oxidase is not yet ready for another transformation because the FAD has gained the H₂. To return to its initial state, the enzyme needs to release that hydrogen molecule:

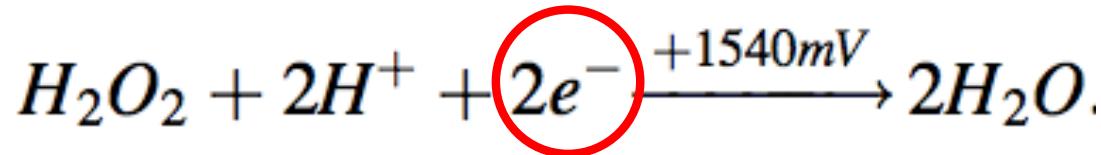


Redox with oxidases

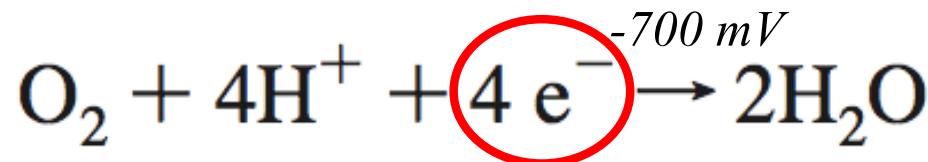
The hydrogen peroxide provide two possible redox reactions. An oxidation:



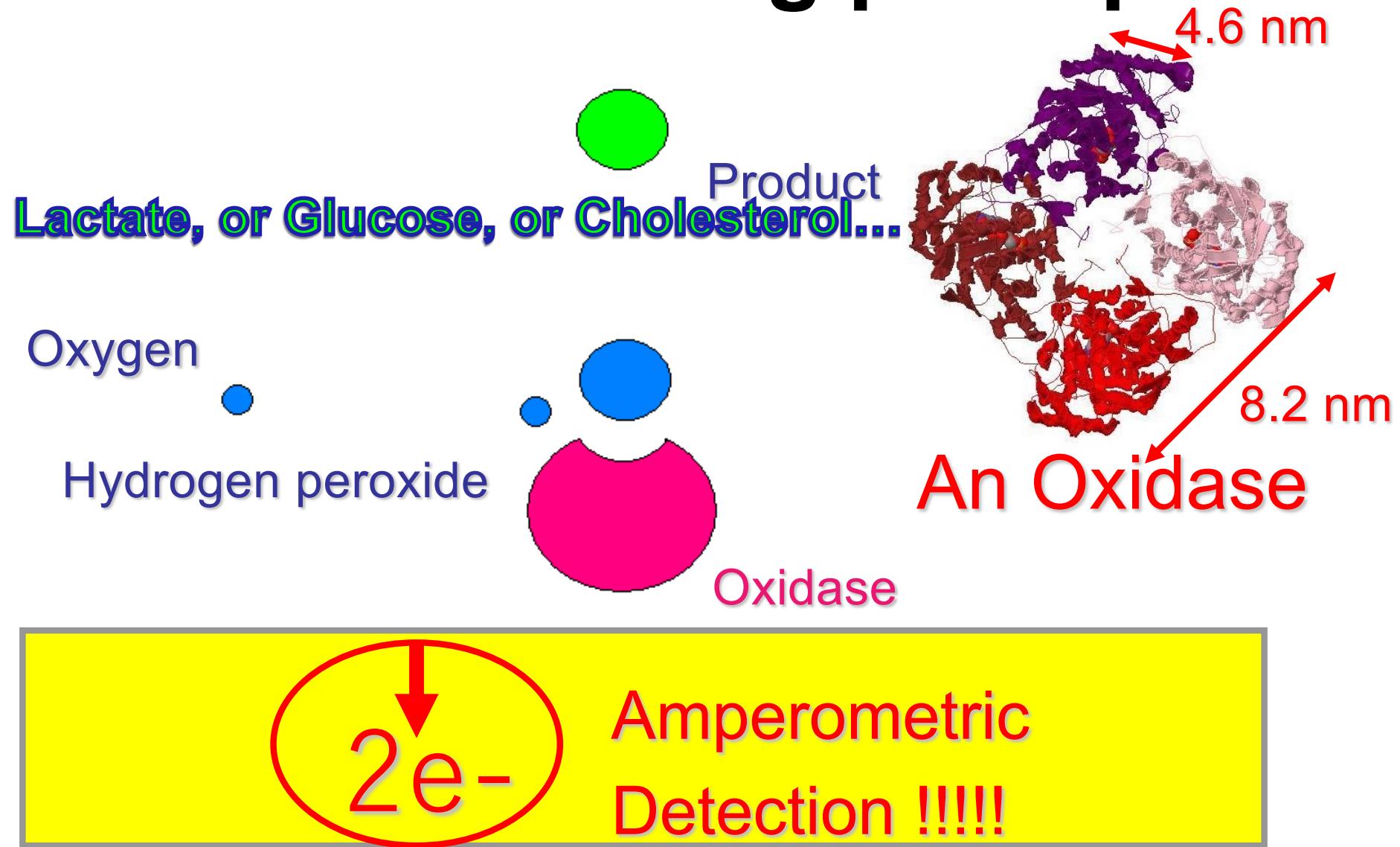
And a reduction:



A third redox is provided by the oxygen reduction:



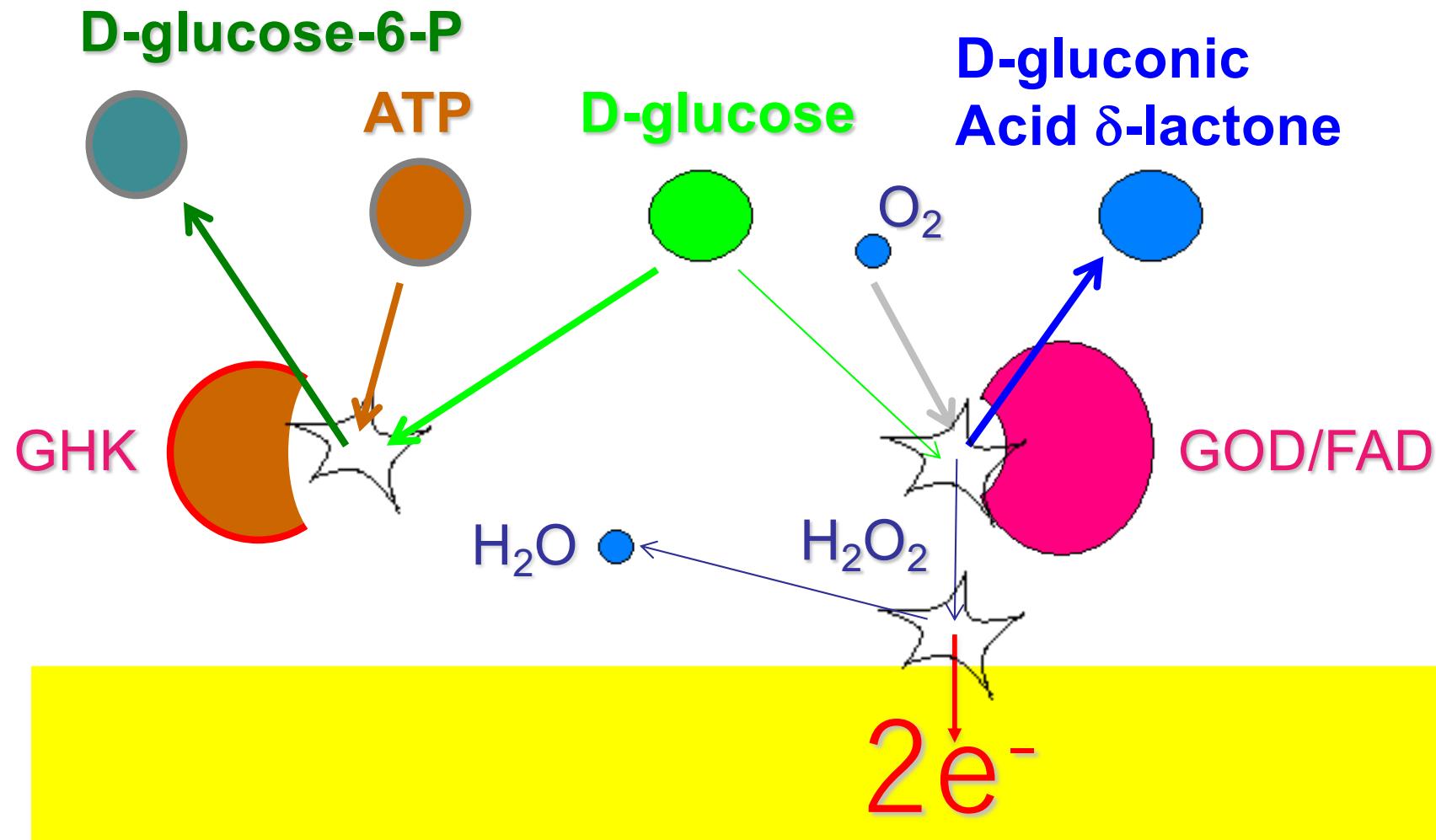
Oxidases working principle



Enzymes' based detection

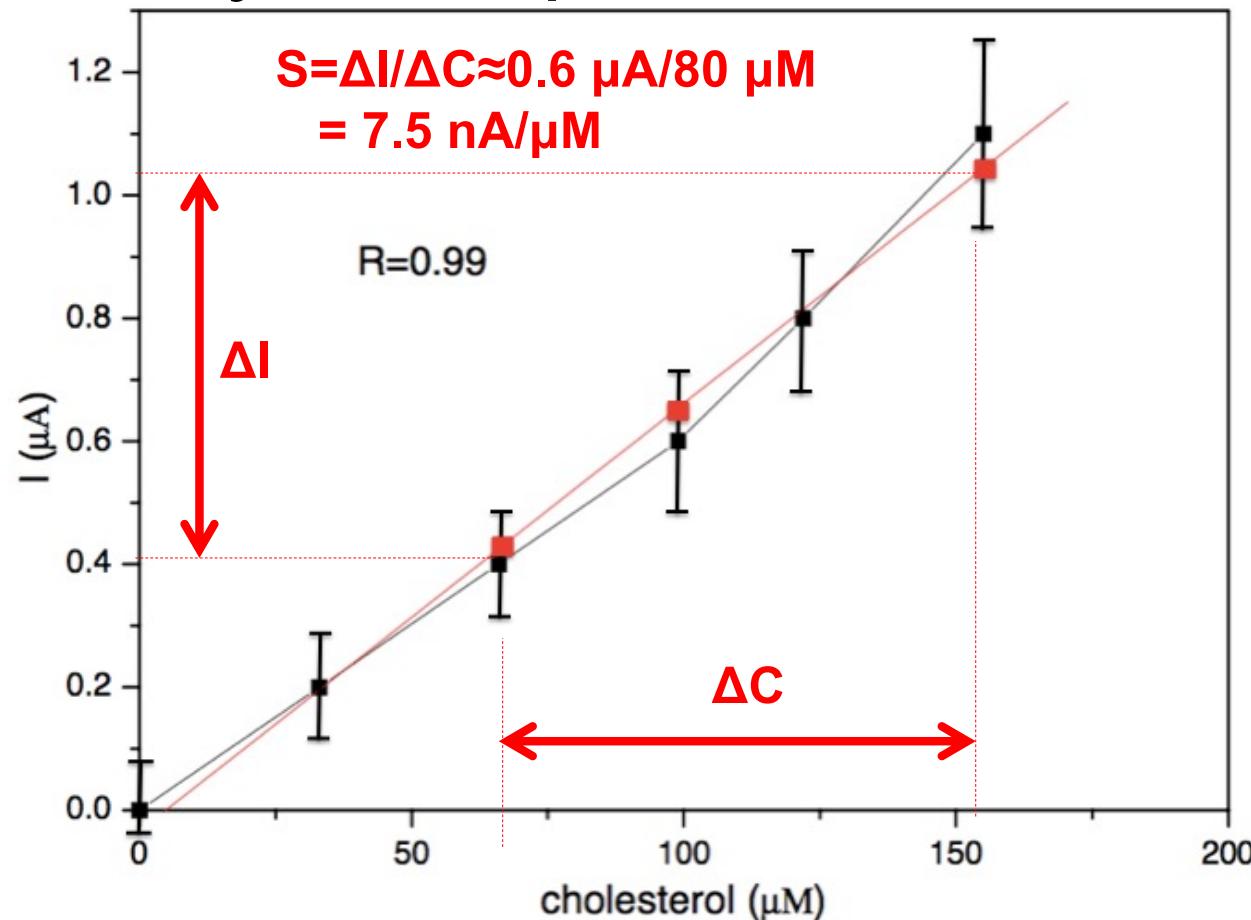
Other enzymes do not provide any redox reaction in catalysing their substrates. However, some of them may be used together with enzyme that do it. In the case, we can exploit their catalysis for the aim of an electrochemical direct detection by combining two different kind of enzymes on the same Bio/CMOS interface. That is the case of the detection of ATP.

ATP detection



Detection Principle

- Sensitivity: example – A linear sensor



Detection Principle

- Detection Limit: a graphic interpretation

